

Designing a Simple Loss Function for the Fed: Does the Dual Mandate Make Sense?*

Davide Debortoli
University of California, San Diego

Jinill Kim
Korea University

Jesper Lindé
Federal Reserve Board and CEPR

Ricardo Nunes
Federal Reserve Board

First version: September 2, 2013

This version: February 14, 2014

Abstract

Yes. Using the workhorse Smets and Wouters (2007) model of the U.S. economy, we find that the role of the output gap should be equal to or even more important than that of inflation when designing a simple loss function to represent household welfare. Moreover, we document that a loss function with nominal wage inflation and the hours gap provides an even better approximation of the true welfare function than a standard objective based on inflation and the output gap. Our results hold up when we introduce interest rate smoothing in the objective to capture the observed gradualism in policy behavior and to ensure that the probability of the federal funds rate hitting the zero lower bound is negligible.

JEL classification: C32, E58, E61.

Keywords: Central banks' objectives, simple loss function, monetary policy design, Smets-Wouters model

*Preliminary and Incomplete. Please do not circulate without the authors permission. We are grateful to Marc Giannoni, Lars Svensson and Andrea Tambalotti for useful discussions, and our discussant Tom Tallarini at the Federal Reserve Macro System Committee meeting in Boston November 2013 for very helpful comments. We also thank seminar participants at Sveriges Riksbank and National Bank of Belgium for useful feedback. Jinill Kim acknowledges the support by Korea Research Foundation Grant funded by the Korean Government (NRF-2013S1A5A2A03044693). The views expressed in this paper are solely the responsibility of the authors and should not be interpreted as reflecting the views of the Board of Governors of the Federal Reserve System or of any other person associated with the Federal Reserve System.

Contact: Debortoli: <ddebortoli@ucsd.edu>; Kim: <jinillkim@korea.ac.kr>; Lindé: <jesper.l.linde@frb.gov>; Nunes: <ricardo.p.nunes@frb.gov>.

1. Introduction

Variable and high rates of price inflation in the 1970s and 1980s caused many economies to delegate the conduct of monetary policy to “instrument-independent” central banks. Drawing on learned experiences, many nations gave their central banks a clear mandate to pursue price stability and instrument independence to achieve it.¹ Early advances in academic research, notably the seminal work of Rogoff (1985) and Persson and Tabellini (1993), supported a strong focus on price stability as a means to enhance the independence and credibility of monetary policymakers. As discussed in further detail in Svensson (2010), an overwhelming majority of these central banks also adopted an explicit inflation target to further strengthen credibility and facilitate accountability. One exception to common central banking practice is the U.S. Federal Reserve, which has since 1977 been assigned a so-called “Dual Mandate” which requires it to “promote maximum employment in a context of price stability”. Only as recent as in January 2012, the Fed finally announced an explicit long-run inflation target, but also made clear its intention to keep a balanced approach between mitigating deviations of inflation from its longer-run goal and deviations of employment from its maximum level.

Although the Fed has established credibility for the long-run inflation target, an important question is whether its heavy focus on resource utilization can be justified. Our reading of the academic literature up to date, perhaps most importantly the work by Woodford (2003), is that resource utilization should be assigned a small weight relative to inflation under the reasonable assumption that the underlying objective of monetary policy is to maximize welfare of the households inhabiting the economy. Drawing on results in Rotemberg and Woodford (1998), Woodford (2003) demonstrated that the objective function of households in a basic New Keynesian sticky-price model could be transformed into a (purely) quadratic function in inflation and the output gap, with the weights determined by the specific features of the economy. With this quadratic objective function, optimization subject to linearized constraints would be sufficient to obtain legitimate results from a normative perspective.² A large literature that followed used these insights to study various aspects of optimal monetary policy. The finding that inflation is a very important goal while resource

¹ The academic literature often distinguishes between *goal-* and *instrument-independent* central banks. Goal independence, i.e. the freedom of the central bank to set its own goals, is difficult to justify in a democratic society. However, instrument independence, i.e. the ability of the central bank to determine the appropriate settings of monetary policy to achieve a given mandate without political interference, is arguably less contentious if the central bank can be held accountable for its actions.

² Some assumptions about efficiency are “unpalatable”, as exemplified by the presence of a positive subsidy that would make the steady state of the market equilibrium equivalent to that of the social planner. This shortcoming was subsequently addressed by e.g. Benigno and Woodford (2006), who extended the LQ transformation to a general setting without the presence of such subsidies.

utilization receives a small weight was largely unchallenged. As a prominent example, Erceg, Henderson and Levin (2000) demonstrated that when both wages and prices are sticky, wage inflation enters into the quadratic approximation with a higher weight than price inflation. The optimal weight on the output gap, however, was still found to be modest.

A potential drawback of the previous literature is that it focused on relatively simple calibrated (or impartially estimated) models. Our goal in this paper is to revisit this issue within the context of an estimated medium-scale model of the U.S. economy. Specifically, we use the workhorse Smets and Wouters (2007) model — SW henceforth — of the U.S. economy to examine how a simple objective for the central bank should be designed in order to approximate the true welfare of households in the model economy as closely as possible. For instance, does the Federal Reserve’s strong focus on resource utilization improve households’ welfare relative to a simple mandate that focuses more heavily on inflation?

Even though it is “optimal” and ideal to implement the Ramsey policy directly, the overview of central banking mandates by Svensson (2010) shows that most advanced countries have not asked their central bank to implement such a policy for society. Instead, many central banks are mandated to follow a simple objective that involves only a small number of economic variables; in the case of the United States, for example, the Federal Reserve follows a dual mandate.³ We believe important reasons for this are that, first, a simple objective facilitates communication of policy actions with the public and makes the conduct of monetary policy more transparent. Second, a simple mandate also enhances accountability of the central bank, which is of key importance. Third and finally, prominent scholars like Svensson (2010) argues that a simple mandate is more robust to model and parameter uncertainty than a complicated state-contingent Ramsey policy.⁴

Following the bulk of the previous literature on the topic, we assume that society can credibly commit to assigning simple objectives to the central bank. We then evaluate how these simple objectives, which are constrained to depend upon only a few variables and have a simple quadratic functional form, perform relative to the Ramsey policy. In that sense, our exercise is similar in spirit to the literature designing simple interest rate rules (see for example Kim and Henderson, 2005, and Schmitt-Grohé and Uribe, 2007). We also assume that the central bank operates under commitment when maximizing its simple objective.⁵ We believe commitment is a good starting point for three

³ The dual mandate was codified only in the Federal Reserve Reform Act of 1977. See Bernanke (2013) for a summary of Federal Reserve’s one hundred years.

⁴ As an alternative to simple mandates, Taylor and Williams (2009) argue in favor of simple and robust policy rules.

⁵ By contrast, Rogoff (1985) considers that the central bank operates under discretion.

reasons. First, the evidence provided by Bodenstein, Hebden and Nunes (2012), Debortoli, Maih and Nunes (forthcoming), and Ilbas (2012) suggests that the Federal Reserve operates with a high degree of commitment; in a choice between commitment and discretion, commitment seems to be the better empirical approximation of Fed behavior. Second, the University of Michigan and Survey of Professional Forecasters measures of long-term expected inflation rates have remained more or less constant during the crisis although the Federal Reserve has communicated a strong emphasis on stabilizing the real economy. Third, since simple interest rate rules as well as Ramsey policy imply commitment, this assumption enables us to directly compare such frameworks with the simple objectives we consider.

As noted earlier, we adopt the SW model in our analysis. This model represents a prominent example of how the U.S. economy can be described by a system of dynamic equations consistent with optimizing behavior. As such, it should be less prone to the Lucas (1976) critique than some prominent studies on optimal monetary policy (see e.g. Rudebusch and Svensson, 1999, and Svensson, 1997).⁶ Moreover, many of the existing papers utilizing models based on optimizing behavior have often relied on simple calibrated models without capital formation.⁷ Even though policy recommendations are model consistent, their relevance may be questioned given the simplicity of these models and the fact that they have not been estimated. By conducting normative analysis with an empirically realistic model, this paper achieves the objective of providing theoretically coherent yet empirically relevant policy recommendations.

A conventional procedure for estimating such a model, following the seminal work of Smets and Wouters (2003), is to form the likelihood function for a first-order approximation of the dynamic equations and use Bayesian priors for the deep parameters. Doing so yields a posterior distribution for the parameters. In a normative analysis that involves an evaluation of a specific criterion function, it may be important to allow for both parameter and model uncertainty.⁸ However, before doing such a fully fledged analysis, we believe it is instructive to start out by performing a normative exercise in the context of a specific model and specific parameter values. We assume that the parameters in the SW model are fixed at their posterior mode, and the optimal policy exercises take as constraints all the SW model equations except the estimated ad hoc monetary policy rule. Instead, the central bank pursues policy to best achieve the objective that it is mandated to accomplish.

⁶ According to Leeper and Zha (2003), the Lucas critique may be less crucial when policy interventions are modest and do not significantly generate important expectations-formation effects.

⁷ See e.g. the classical paper by Clarida, Gali and Gertler (1999).

⁸ See Walsh (2005) as an example.

Our main findings are as follows. First, we find that adding a term involving a measure of real activity appears to be much more important than previously thought. A positive weight on any of the typical variables like the output gap, the level of output, and the growth rate of output improves welfare significantly; but among them, the model-consistent output gap performs the best. Specifically, we find that in a simple loss function — with the weight on annualized core inflation normalized to unity — the optimized weight on the output gap is about 1. This is considerably higher than the reference value of 0.048 derived in the graduate textbook of Woodford (2003) and the value of 0.25 assumed by Yellen (2012).⁹ Our basic finding that the central bank should respond vigorously to resource utilization is consistent with the arguments in Reifschneider, Wascher and Wilcox (2013) and English, López-Salido and Tetlow (2013).

At first glance, our results may seem contradictory to Justiniano, Primiceri and Tambalotti (2013), who argue that there is no important trade-off between stabilizing inflation and the output gap. However, the different findings can be reconciled by recognizing that the key drivers behind the trade-off in the SW model—the price- and wage-markup shocks—are absent in the baseline model analyzed by Justiniano, Primiceri and Tambalotti (2013). While the evidence presented by these authors against the wage markup shock is compelling, we notice that our main results hold up even if we omit the wage markup shock, because the price-markup shock by itself creates an important trade-off. And regarding this shock, we find the analysis in Justiniano et al. less of a clear cut; they suppress the need for this shock with their assumption that movements in inflation are largely driven by exogenous movements in the Fed’s inflation target. While arguments can be made against each specification, our results can be interpreted as providing a complementary analysis to theirs, and we demonstrate that our findings are relevant even if only a relatively small portion of the variance of price and wage inflation are indeed driven by the inefficient price- and wage-markup shocks.

Our second important finding is that a loss function with wage inflation and the hours gap provides an even better approximation to the household true welfare function than a simple standard inflation-output gap based objective. As is the case with the inflation-output gap based simple objective, the hours gap, defined as the difference between actual and potential hours worked per capita, should be assigned a large weight in such a loss function. The reason why targeting labor market variables provides a better approximation of the Ramsey policy is that the labor market in the SW model features nominal wage frictions and mark-up shocks.

⁹ Yellen (2012) assumed a value of unity for the unemployment gap, which by the Okun’s law translates into a value of 0.25 for the output gap.

Third, we show that our basic result is robust to a number of important perturbations of the simple loss function; notably when imposing realistic limitations on the extent to which monetary policy makers change policy interest rates. Fourth and finally, we find that simple interest rate rules which allow for interest rate smoothing and the level and change of the resource utilization measure (either the output gap or the hours gap) approximate Ramsey policy about equally well as the simple mandates.

This paper proceeds as follows. We start by presenting the SW model and describe how to compute the Ramsey policy and to evaluate the alternative monetary policies. Section 3 reports our benchmark results. The robustness of our results along some key dimensions are subsequently discussed in Section 4, while the comparison with simple rules is discussed in Section 5. Finally, Section 6 provides some concluding remarks and suggestions for further research.

2. The Model and Our Exercise

In this section, we lay out the model we use and describe our exercise to find optimized simple objectives.

2.1. The Smets and Wouters (2007) Model

Below, we describe the firms' and households' problem in the model, and state the market clearing conditions.¹⁰ The discussion about the conduct of monetary policy is deferred to Section 2.2.

2.1.1. Firms and Price Setting

Final Goods Production The single final output good Y_t is produced using a continuum of differentiated intermediate goods $Y_t(f)$. Following Kimball (1995), the technology for transforming these intermediate goods into the final output good is

$$\int_0^1 G_Y \left(\frac{Y_t(f)}{Y_t} \right) df = 1. \quad (1)$$

Following Dotsey and King (2005) and Levin, Lopez-Salido and Yun (2007) we assume that $G_Y(\cdot)$ is given by a strictly concave and increasing function; its particular parameterization follows SW:

$$G_Y \left(\frac{Y_t(f)}{Y_t} \right) = \left(\frac{\phi_p}{1-(\phi_p-1)\epsilon_p} \left[\left(\frac{\phi_p+(1-\phi_p)\epsilon_p}{\phi_p} \right) \frac{Y_t(f)}{Y_t} + \frac{(\phi_p-1)\epsilon_p}{\phi_p} \right]^{\frac{1-(\phi_p-1)\epsilon_p}{\phi_p-(\phi_p-1)\epsilon_p}} + \left[1 - \frac{\phi_p}{1-(\phi_p-1)\epsilon_p} \right] \right), \quad (2)$$

¹⁰ For a more detailed description of the model, we refer the reader to the on-line appendix of the Smets and Wouters paper, which is available online at http://www.aeaweb.org/aer/data/june07/20041254_app.pdf.

where $\phi_p \geq 1$ denotes the gross markup of the intermediate firms. The parameter ϵ_p governs the degree of curvature of the intermediate firm's demand curve. When $\epsilon_p = 0$, the demand curve exhibits constant elasticity as with the standard Dixit-Stiglitz aggregator. When ϵ_p is positive—as in SW—the firms instead face a quasi-kinked demand curve, implying that a drop in its relative price only stimulates a small increase in demand. On the other hand, a rise in its relative price generates a large fall in demand. Relative to the standard Dixit-Stiglitz aggregator, this introduces more strategic complementarity in price setting which causes intermediate firms to adjust prices less to a given change in marginal cost. Finally, notice that $G_Y(1) = 1$, implying constant returns to scale when all intermediate firms produce the same amount.

Firms that produce the final output good are perfectly competitive in both the product and factor markets. Thus, final goods producers minimize the cost of producing a given quantity of the output index Y_t , taking as given the price $P_t(f)$ of each intermediate good $Y_t(f)$. Moreover, final goods producers sell units of the final output good at a price P_t , and hence solve the following problem:

$$\max_{\{Y_t, Y_t(f)\}} P_t Y_t - \int_0^1 P_t(f) Y_t(f) df \quad (3)$$

subject to the constraint (1). The first order conditions for this problem can be written

$$\begin{aligned} \frac{Y_t(f)}{Y_t} &= \frac{\phi_p}{\phi_p - (\phi_p - 1)\epsilon_p} \left(\left[\frac{P_t(f)}{P_t} \frac{1}{\Lambda_t^p} \right]^{-\frac{\phi_p - (\phi_p - 1)\epsilon_p}{\phi_p - 1}} + \frac{(1 - \phi_p)\epsilon_p}{\phi_p} \right), \\ P_t \Lambda_t^p &= \left[\int P_t(f)^{-\frac{1 - (\phi_p - 1)\epsilon_p}{\phi_p - 1}} df \right]^{-\frac{\phi_p - 1}{1 - (\phi_p - 1)\epsilon_p}}, \\ \Lambda_t^p &= 1 + \frac{(1 - \phi_p)\epsilon_p}{\phi_p} - \frac{(1 - \phi_p)\epsilon_p}{\phi_p} \int \frac{P_t(f)}{P_t} df, \end{aligned} \quad (4)$$

where Λ_t^p denotes the Lagrange multiplier on the aggregator constraint (1). Note that for $\epsilon_p = 0$ and $\Lambda_t^p = 1$ in each period t , the demand and pricing equations collapse to the usual Dixit-Stiglitz expressions

$$\frac{Y_t(f)}{Y_t} = \left[\frac{P_t(f)}{P_t} \right]^{-\frac{\phi_p}{\phi_p - 1}}, P_t = \left[\int P_t(f)^{\frac{1}{1 - \phi_p}} df \right]^{1 - \phi_p}. \quad (5)$$

Intermediate Goods Production A continuum of intermediate goods $Y_t(f)$ for $f \in [0, 1]$ is produced by monopolistically competitive firms, each of which produces a single differentiated good. Each intermediate goods producer faces the demand schedule in eq. (4) from the final goods firms through the solution to the problem in (3), which varies inversely with its output price $P_t(f)$ and directly with aggregate demand Y_t .

Each intermediate goods producer utilizes capital services $K_t(f)$ and a labor index $L_t(f)$ (defined below) to produce its respective output good. The form of the production function is Cobb-Douglas:

$$Y_t(f) = \varepsilon_t^a K_t(f)^\alpha [\gamma^t L_t(f)]^{1-\alpha} - \gamma^t \Phi, \quad (6)$$

where γ^t represents the labour-augmenting deterministic growth rate in the economy, Φ denotes the fixed cost (which is related to the gross markup ϕ_p so that profits are zero in the steady state), and ε_t^a is total factor productivity which follows the process

$$\ln \varepsilon_t^a = (1 - \rho_a) \ln \varepsilon^a + \rho_a \ln \varepsilon_{t-1}^a + \eta_t^a, \eta_t^a \sim N(0, \sigma_a). \quad (7)$$

Firms face perfectly competitive factor markets for renting capital and hiring labor. Thus, each firm chooses $K_t(f)$ and $L_t(f)$, taking as given both the rental price of capital R_{Kt} and the aggregate wage index W_t (defined below). Firms can costlessly adjust either factor of production. Thus, the standard static first-order conditions for cost minimization imply that all firms have identical marginal cost per unit of output.

The prices of the intermediate goods are determined by Calvo-Yun (1996) style staggered nominal contracts. In each period, each firm f faces a constant probability, $1 - \xi_p$, of being able to reoptimize its price $P_t(f)$. The probability that any firm receives a signal to re-optimize its price is assumed to be independent of the time that it last reset its price. If a firm is not allowed to optimize its price in a given period, it adjusts its price by a weighted combination of the lagged and steady-state rate of inflation, i.e., $P_t(f) = (1 + \pi_{t-1})^{\iota_p} (1 + \pi)^{1-\iota_p} P_{t-1}(f)$ where $0 \leq \iota_p \leq 1$ and π_{t-1} denotes net inflation in period $t-1$, and π the steady-state net inflation rate. A positive value of ι_p introduces structural inertia into the inflation process. All told, this leads to the following optimization problem for the intermediate firms

$$\max_{\tilde{P}_t(f)} E_t \sum_{j=0}^{\infty} (\beta \xi_p)^j \frac{\Xi_{t+j} P_t}{\Xi_t P_{t+j}} \left[\tilde{P}_t(f) \left(\Pi_{s=1}^j (1 + \pi_{t+s-1})^{\iota_p} (1 + \pi)^{1-\iota_p} \right) - MC_{t+j} \right] Y_{t+j}(f), \quad (8)$$

where $\tilde{P}_t(f)$ is the newly set price. Notice that with our assumptions all firms that re-optimize their prices actually set the same price.

Because a non-linear version of the model cannot be written in a recursive form when the markup in (2) becomes time-varying as in the SW model, we instead directly introduce a shock ε_t^p in the the first-order condition to the problem in (8). And following SW, we assume the shock is given by an exogenous ARMA(1,1) process:

$$\ln \varepsilon_t^p = (1 - \rho_p) \ln \varepsilon^p + \rho_p \ln \varepsilon_{t-1}^p + \eta_t^p - \mu_p \eta_{t-1}^p, \eta_t^p \sim N(0, \sigma_p). \quad (9)$$

When this shock is introduced in the non-linear model, we put a scaling factor on it so that it enters exactly the same way in a log-linearized representation of the model as the price markup shock does in the SW model.¹¹

2.1.2. Households and Wage Setting

We assume a continuum of monopolistically competitive households (indexed on the unit interval), each of which supplies a differentiated labor service to the production sector; that is, goods-producing firms regard each household's labor services $L_t(h)$, $h \in [0, 1]$, as imperfect substitutes for the labor services of other households. It is convenient to assume that a representative labor aggregator combines households' labor hours in the same proportions as firms would choose. Thus, the aggregator's demand for each household's labor is equal to the sum of firms' demands. The aggregated labor index L_t has the Kimball (1995) form:

$$L_t = \int_0^1 G_L \left(\frac{L_t(h)}{L_t} \right) dh = 1 \quad (10)$$

where the function $G_L(\cdot)$ has the same functional form as (2), but is characterized by the corresponding parameters ϵ_w (governing convexity of labor demand by the aggregator) and ϕ_w (gross wage markup). The aggregator minimizes the cost of producing a given amount of the aggregate labor index L_t , taking each household's wage rate $W_t(h)$ as given, and then sells units of the labor index to the intermediate goods sector at unit cost W_t , which can naturally be interpreted as the aggregate wage rate. From the FOCs, the aggregator's demand for the labor hours of household h —or equivalently, the total demand for this household's labor by all goods-producing firms—is given by

$$\frac{L_t(h)}{L_t} = G_L'^{-1} \left[\frac{W_t(h)}{W_t} \int_0^1 G_L' \left(\frac{L_t(h)}{L_t} \right) \frac{L_t(h)}{L_t} dh \right], \quad (11)$$

where $G_L'(\cdot)$ denotes the derivative of the $G_L(\cdot)$ function in eq. (10).

The utility function of a typical member of household h is

$$E_t \sum_{j=0}^{\infty} \beta^j \left[\frac{1}{1 - \sigma_c} (C_{t+j}(h) - \kappa C_{t+j-1}) \right]^{1 - \sigma_c} \exp \left(\frac{\sigma_c - 1}{1 + \sigma_l} L_{t+j}(h)^{1 + \sigma_l} \right) \quad (12)$$

¹¹Alternatively, we could have followed the specification in Adjemian et al. (2008) and introduced the shock as a tax on the intermediate firm's revenues in the problem (8) directly. The drawback with this alternative approach is that the log-linearized representation of the model would have a different lead-lag structure from the representation in SW. In a later section, we perform robustness analysis with respect to the price- and wage-markup shocks and show that our main result holds.

where the discount factor β satisfies $0 < \beta < 1$.¹² The period utility function depends on household h 's current consumption $C_t(h)$, as well as lagged aggregate per capita consumption to allow for external habit persistence. The period utility function also depends inversely on hours worked $L_t(h)$.

Household h 's budget constraint in period t states that its expenditure on goods and net purchases of financial assets must equal its disposable income:

$$\begin{aligned} P_t C_t(h) + P_t I_t(h) + \frac{B_{t+1}(h)}{\varepsilon_t^b R_t} + \int_s \xi_{t,t+1} B_{D,t+1}(h) - B_{D,t}(h) \\ = B_t(h) + W_t(h) L_t(h) + R_t^k Z_t(h) K_t^p(h) - a(Z_t(h)) K_t^p(h) + \Gamma_t(h) - T_t(h) \end{aligned} \quad (13)$$

Thus, the household purchases part of the final output good (at a price of P_t), which it chooses either to consume $C_t(h)$ or invest $I_t(h)$ in physical capital. Following Christiano, Eichenbaum, and Evans (2005), investment augments the household's (end-of-period) physical capital stock $K_{t+1}^p(h)$ according to

$$K_{t+1}^p(h) = (1 - \delta) K_t^p(h) + \varepsilon_t^i \left[1 - S \left(\frac{I_t(h)}{I_{t-1}(h)} \right) \right] I_t(h). \quad (14)$$

The extent to which investment by each household h turns into physical capital is assumed to depend on an exogenous shock ε_t^i and how rapidly the household changes its rate of investment according to the function $S \left(\frac{I_t(h)}{I_{t-1}(h)} \right)$, which we specify as

$$S(x_t) = \frac{\varphi}{2} (x_t - \gamma)^2. \quad (15)$$

Notice that this function satisfies $S(\gamma) = 0$, $S'(\gamma) = 0$ and $S''(\gamma) = \varphi$. The stationary investment-specific shock ε_t^i follows

$$\ln \varepsilon_t^i = \rho_i \ln \varepsilon_{t-1}^i + \eta_t^i, \eta_t^i \sim N(0, \sigma_i). \quad (16)$$

In addition to accumulating physical capital, households may augment their financial assets through increasing their government nominal bond holdings (B_{t+1}), from which they earn an interest rate of R_t . The return on these bonds is also subject to a risk-shock, ε_t^b , which follows

$$\ln \varepsilon_t^b = \rho_b \ln \varepsilon_{t-1}^b + \eta_t^b, \eta_t^b \sim N(0, \sigma_b). \quad (17)$$

We assume that agents can engage in frictionless trading of a complete set of contingent claims to diversify away idiosyncratic risk. The term $\int_s \xi_{t,t+1} B_{D,t+1}(h) - B_{D,t}(h)$ represents net pur-

¹² Note that we deviate slightly from the notation in SW by using h to index households and using $\varkappa$ to denote the degree of habit formation.

chases of these state-contingent domestic bonds, with $\xi_{t,t+1}$ denoting the state-dependent price, and $B_{D,t+1}(h)$ the quantity of such claims purchased at time t .

On the income side, each member of household h earns after-tax labor income $W_t(h) L_t(h)$, after-tax capital rental income of $R_t^k Z_t(h) K_t^p(h)$, and pays a utilization cost of the physical capital equal to $a(Z_t(h)) K_t^p(h)$ where $Z_t(h)$ is the capital utilization rate, so that capital services provided by household h , $K_t(h)$, equals $Z_t(h) K_t^p(h)$. The capital utilization adjustment function $a(Z_t(h))$ is assumed to be given by

$$a(Z_t(h)) = \frac{r^k}{\tilde{z}_1} [\exp(\tilde{z}_1 (Z_t(h) - 1)) - 1], \quad (18)$$

where r^k is the steady state net real interest rate ($\bar{R}_t^K / \bar{P}_t$). Notice that the adjustment function satisfies $a(1) = 0$, $a'(1) = r^k$, and $a''(1) \equiv r^k \tilde{z}_1$. Following SW, we want to write $a''(1) = z_1 = \psi / (1 - \psi) > 0$, where $\psi \in [0, 1)$ and a higher value of ψ implies a higher cost of changing the utilization rate. Our parameterization of the adjustment cost function then implies that we need to set $\tilde{z}_1 \equiv z_1 / r^k$. Finally, each member also receives an aliquot share $\Gamma_t(h)$ of the profits of all firms, and pays a lump-sum tax of $T_t(h)$ (regarded as taxes net of any transfers).

In every period t , each member of household h maximizes the utility function (12) with respect to its consumption, investment, (end-of-period) physical capital stock, capital utilization rate, bond holdings, and holdings of contingent claims, subject to its labor demand function (11), budget constraint (13), and transition equation for capital (14).

Households also set nominal wages in Calvo-style staggered contracts that are generally similar to the price contracts described previously. Thus, the probability that a household receives a signal to re-optimize its wage contract in a given period is denoted by $1 - \xi_w$. In addition, SW specify the following dynamic indexation scheme for the adjustment of the wages of those households that do not get a signal to re-optimize: $W_t(h) = \gamma (1 + \pi_{t-1})^{\iota_w} (1 + \pi)^{1-\iota_w} W_{t-1}(h)$. All told, this leads to the following optimization problem for the households

$$\max_{\tilde{W}_t(h)} E_t \sum_{j=0}^{\infty} (\beta \xi_w)^j \frac{\Xi_{t+j} P_t}{\Xi_t P_{t+j}} \left[\tilde{W}_t(h) \left(\prod_{s=1}^j \gamma (1 + \pi_{t+s-1})^{\iota_w} (1 + \pi)^{1-\iota_w} \right) - W_{t+j} \right] L_{t+j}(h), \quad (19)$$

where $\tilde{W}_t(h)$ is the newly set wage; notice that with our assumptions all households that reoptimize their wages will actually set the same wage.

Following the same approach as with the intermediate goods firms, we introduce a shock ε_t^w in the resulting first-order condition. This shock, following SW, is assumed to be given by an

exogenous ARMA(1,1) process

$$\ln \varepsilon_t^w = (1 - \rho_w) \ln \varepsilon^w + \rho_w \ln \varepsilon_{t-1}^w + \eta_t^w - \mu_w \eta_{t-1}^w, \eta_t^w \sim N(0, \sigma_w). \quad (20)$$

As discussed previously, we use a scaling factor for this shock so that it enters in exactly the same way as the wage markup shock in SW in the log-linearized representation of the model.

2.1.3. Market Clearing Conditions

Government purchases G_t are exogenous, and the process for government spending relative to trend output, i.e. $g_t = G_t / (\gamma^t Y)$, is given by the following exogenous AR(1) process:

$$\ln g_t = (1 - \rho_g) \ln g + \rho_g (\ln g_{t-1} - \rho_{ga} \ln \varepsilon_{t-1}^a) + \varepsilon_t^g, \varepsilon_t^g \sim N(0, \sigma_g) \quad (21)$$

Government purchases have no effect on the marginal utility of private consumption, nor do they serve as an input into goods production. The consolidated government sector budget constraint is

$$\frac{B_{t+1}}{R_t} = G_t - T_t + B_t \quad (22)$$

By comparing the debt terms in the household budget constraint in eq. (13) with the equation above, one can see that receipts from the risk shock are subject to iceberg costs, and hence do not add any income to the government.¹³

Total output of the final goods sector is used as follows:

$$Y_t = C_t + I_t + G_t + a(Z_t) \bar{K}_t, \quad (23)$$

where $a(Z_t) \bar{K}_t$ is the capital utilization adjustment cost.

Finally, we need to specify the aggregate production constraint. To do that, we note that the unweighted sum of the intermediate firms' output equals

$$Y_t^{sum} = \int_0^1 Y_t(f) df, \quad (24)$$

which from eq. (6) can be rewritten as

$$\begin{aligned} Y_t^{sum} &= \int_0^1 \left[\varepsilon_t^a K_t(f)^\alpha [\gamma^t L_t(f)]^{1-\alpha} - \gamma^t \Phi \right] df \\ &= \varepsilon_t^a \left(\frac{K_t}{\gamma^t L_t} \right)^\alpha \int_0^1 \gamma^t L_t(f) df - \gamma^t \Phi \end{aligned} \quad (25)$$

¹³ But even if they did, it would not matter as we follow SW and assume that the government balances its expenditures each period through lump-sum taxes, $T_t = G_t + B_t - B_{t+1}/R_t$, so that government debt $B_t = 0$ in equilibrium. Furthermore, as Ricardian equivalence holds in the model, it does not matter for equilibrium allocations whether the government balances its debt or not in each period.

where the second equality follows from the fact that every firms capital-labor ratio will be the same in equilibrium.

From the first-order conditions to the final goods aggregator problem (4), it follows that

$$Y_t^{sum} = Y_t \int_0^1 \frac{\phi_p}{\phi_p - (\phi_p - 1)\epsilon_p} \left(\left[\frac{P_t(f)}{P_t} \frac{1}{\Lambda_t^p} \right]^{-\frac{\phi_p - (\phi_p - 1)\epsilon_p}{\phi_p - 1}} + \frac{(1 - \phi_p)\epsilon_p}{\phi_p} \right) df, \quad (26)$$

so that

$$\varepsilon_t^a \left(\frac{K_t}{\gamma^t L_t} \right)^\alpha \gamma^t \int_0^1 L_t(h) dh - \gamma^t \Phi = Y_t \int_0^1 \frac{\phi_p}{\phi_p - (\phi_p - 1)\epsilon_p} \left(\left[\frac{P_t(f)}{P_t} \frac{1}{\Lambda_t^p} \right]^{-\frac{\phi_p - (\phi_p - 1)\epsilon_p}{\phi_p - 1}} + \frac{(1 - \phi_p)\epsilon_p}{\phi_p} \right) df.$$

By inserting the expression for the unweighted sum of labor, $\int_0^1 \gamma^t L_t(h) dh$, into this last expression, we can finally derive the aggregate production constraint which depends of aggregate technology, capital, labor, fixed costs, as well as the price and wage dispersion terms.¹⁴

2.1.4. Model Parameterization

When solving the model, we adopt the parameter estimates (posterior mode) in Tables 1.A and 1.B of SW. We also use the same values for the calibrated parameters. Table 1 provides the relevant values.

There are two issues to notice with regards to the parameters in Table 1. First, we adapt and re-scale the processes of the price and wage markup shocks so that when our model is log-linearized it matches exactly the original SW model. Second, we set the monetary policy shock parameters to nil, as we restrict our analysis to optimal policy.

¹⁴ We refer the interested reader to Adjemian, Paries and Moyen (2008) for further details.

Table 1: Parameter Values in Smets and Wouters (2007).

Panel A: Calibrated					
Parameter	Description	Value	Parameter	Description	Value
δ	Depreciation rate	0.025	ϵ_p	Kimball Elas. GM	10
ϕ_w	Gross wage markup	1.50	ϵ_w	Kimball Elast. LM	10
g_y	Gov't G/Y ss-ratio	0.18			
Panel B: Estimated					
Parameter	Description	Value	Parameter	Description	Value
φ	Investment adj. cost	5.48	α	Capital production share	0.19
σ_c	Inv subs. elas. of cons.	1.39	ψ	Capital utilization cost	0.54
$\varkappa$	Degree of ext. habit	0.71	ϕ_p	Gross price markup	1.61
ξ_w	Calvo prob. wages	0.73	π	Steady state net infl. rate	0.0081
σ_l	Labor supply elas.	1.92	β	Discount factor	0.9984
ξ_p	Calvo prob. prices	0.65	$\bar{l}$	Steady state hours worked	0.25
ι_w	Ind. for non-opt. wages	0.59	γ	Steady state gross growth	1.0043
ι_p	Ind. for non-opt. prices	0.22			
Panel C: Shock Processes					
Shock	Persistence	MA(1)		Std. of Innovation (%)	
Neutral Technology	ρ_a	0.95	-	σ_a	0.45
Risk premium	ρ_b	0.18	-	σ_b	0.24
Gov't spending	ρ_g	0.97	ρ_{ga} 0.52	σ_g	0.52
Inv. Specific Tech.	ρ_i	0.71		σ_i	0.45
Price markup	ρ_p	0.90	μ_p 0.74	σ_p	0.14
Wage markup	ρ_w	0.97	μ_w 0.88	σ_w	0.24
Monetary policy	ρ_r	-	-	σ_r	-

Note: SW estimates $\rho_r = 0.12$ and $\sigma_r = 0.24$, but in our optimal policy exercises these parameters are not present.

2.2. Methodology for Optimized Simple Objectives

Rotemberg and Woodford (1998) showed that—under the assumption that the steady state satisfies certain efficiency conditions—the objective function of households can be transformed into a (purely) quadratic function using the first-order properties of the constraints. With this quadratic objective function, optimization subject to linearized constraints would be sufficient to obtain legitimate results from a normative perspective. Some assumptions about efficiency were “unpalatable” as exemplified by the presence of positive subsidies that would make the steady state of the market equilibrium equivalent to that of the social planner.¹⁵ Therefore, many researchers — including Benigno and Woodford (2006) — extended the LQ transformation to a general setting without the presence of such subsidies. Benigno and Woodford (2006) demonstrated that the objective function

¹⁵ Even when theoretical research papers imposed this assumption, most prominent empirically oriented papers including Christiano, Eichenbaum and Evans (2005) and Smets and Wouters (2003, 2007) did not assume the existence of such positive subsidies.

of the households could be transformed into a (purely) quadratic form:

$$\sum_{t=0}^{\infty} E_0 [\beta^t U(X_t)] \simeq \text{constant} - \sum_{t=0}^{\infty} E_0 [\beta^t X_t' W^{society} X_t], \quad (27)$$

where X_t is a $N \times 1$ vector with model variables measured as their deviation from the steady state; therefore, $X_t' W^{society} X_t$ is referred to as the linear-quadratic approximation of the household utility function $U(X_t)$. The difference from Rotemberg and Woodford (1998) is that this general transformation needs to utilize the second-order properties of the constraints as well as their first-order properties in order to properly account for the fact that we are allowing for a non-efficient steady state.

We define Ramsey policy as a policy which maximizes (27) subject to the $N - 1$ constraints of the economy. While N is the number of variables, there are only $N - 1$ constraints provided by the SW model because the monetary policy rule is omitted. Unlike the efficient steady-state case of Rotemberg and Woodford (1998), second-order terms of the constraints do influence the construction of the $W^{society}$ matrix in (27), and as explained in Section 2.1 we made assumptions on the functional forms for the various adjustment functions (for example, the capital utilization rate $a(Z_t)$, the investment adjustment cost function $S(I_t/I_{t-1})$, and the Kimball aggregators) that are consistent with the linearized behavioral equations in SW.

Since the constant term in (27) depends only on the steady state which is invariant across different policies considered in this paper, the optimal policy implemented by a Ramsey planner can be solved as

$$\tilde{X}_t^{optimal} (W^{society}; \tilde{X}_{t-1}) = \arg \min_{X_t} E_0 \left[\sum_{t=0}^{\infty} \beta^t X_t' W^{society} X_t \right], \quad (28)$$

where the minimization is subject to the $N - 1$ constraints in the economy, which are omitted for brevity. Following Marcet and Marimon (2012), the lagrange multipliers associated with the constraints become state variables. Accordingly $\tilde{X}_t' \equiv [X_t' \varpi_t']$ now includes the Lagrange multipliers ϖ_t as well. For expositional ease we denote these laws of motion more compactly as $\tilde{X}_t^{optimal} (W^{society})$.

Using (27) to evaluate welfare would require taking a stance on the initial conditions. Doing so is particularly challenging when lagrange multipliers are part of the vector of state variables because these are not readily interpretable. We therefore adopt the unconditional expectations operator as

a basis for welfare evaluation.¹⁶ The loss under Ramsey optimal policy is then defined by

$$Loss^{Ramsey} = E \left[\left(X_t^{optimal} (W^{society}) \right)' W^{society} \left(X_t^{optimal} (W^{society}) \right) \right]. \quad (29)$$

Our choice of an unconditional expectation as the welfare measure is standard in the literature (see for instance Woodford, 2003). Furthermore, when the discount factor is close to unity – as is the case in our calibration – unconditional and conditional welfare are also quite similar.¹⁷

The Ramsey policy is a useful benchmark. Obviously, in theory a society could design a mandate equal to the Ramsey objective (27). But in practice most societies do not; instead, most central banks are subject to a mandate involving only a few variables. To capture this, we assume society provides the central bank with a loss function

$$E_0 \left[\sum_{t=0}^{\infty} \beta^t X_t' W^{CB} X_t \right], \quad (30)$$

where W^{CB} is a sparse matrix with only a few non-zero entries. The matrix W^{CB} summarizes the simple mandates and will be specified in detail in our analysis. Given a simple mandate, the optimal behavior of the central bank is

$$\tilde{X}_t^{optimal} (W^{CB}; \tilde{X}_{t-1}) = \arg \min_{X_t} E_0 \left[\sum_{t=0}^{\infty} \beta^t X_t' W^{CB} X_t \right]. \quad (31)$$

When the simple mandate does not coincide with the Ramsey policy, we have that $W^{CB} \neq W^{society}$ and therefore that $\tilde{X}_t^{optimal} (W^{CB}) \neq \tilde{X}_t^{optimal} (W^{society})$. To compute the extent to which the simple mandate of the central bank approximates optimal policy, one can calculate its associated loss according to the formula:

$$Loss^{objective} (W^{CB}) = E \left[\left(X_t^{optimal} (W^{CB}) \right)' W^{society} \left(X_t^{optimal} (W^{CB}) \right) \right]. \quad (32)$$

The welfare performance of the simple mandate is then found by taking the difference between $Loss^{objective}$ in eq. (32) and $Loss^{Ramsey}$ in eq. (29). In our presentation of the results, we express this welfare difference in consumption equivalent variation (CEV) units as follows:

$$CEV = 100 \left(\frac{Loss^{objective} - Loss^{Ramsey}}{\bar{C} \left(\frac{\partial U}{\partial C} |_{s.s.} \right)} \right), \quad (33)$$

¹⁶ See Jensen and McCallum (2010) for a detailed discussion about this criterion—with a comparison to the timeless perspective. They motivate the optimal unconditional continuation policy based on the presence of time inconsistency, since the policy would reap the credibility gains successfully. We note, however, that our approach does not exactly follow theirs in that their optimal steady state could be different from the steady state under the Ramsey policy in a model with steady-state distortions.

¹⁷ The unconditional criterion is equivalent to maximization of the conditional welfare when the society's discount factor, $\tilde{\beta}$ in the expression $(1 - \tilde{\beta})^{-1} E_0 \left[\sum \tilde{\beta}^t \left[\tilde{X}_t^{CB} (W^{CB}; \tilde{X}_{t-1}) \right]' W^{society} \left[\tilde{X}_t^{CB} (W^{CB}; \tilde{X}_{t-1}) \right] \right]$, is approaching unity. In our case, we have that $\beta \gamma^{-\sigma_c} = 0.993$ based on the parameter values in Table 1.

where $\bar{C} \left(\frac{\partial U}{\partial C} |_{s.s.} \right)$ can be interpreted as how much welfare increases when consumption in the steady state is increased by one percent. That is, CEV represents the percentage point increase in households' consumption, in every period and state of the world, that makes them—in expectation—equally well-off under the simple mandate as they would be under Ramsey policy.¹⁸ Moreover, (33) makes clear that our choice to neglect the policy-invariant constant in (27) when deriving the Ramsey policy in (28) is immaterial for the results in our paper since all alternative policies are evaluated as difference from the loss under Ramsey.

So far we proceeded under the assumption that the law governing the behavior of the central bank specifies both the variables and the weights in the quadratic objective, i.e. W^{CB} in (30). But in practice, the mandates of central banks are only indicative and not entirely specific on the weights that should be attached to each of the target variables. A straightforward way to model this is to assume that society designs a law Ω with

$$\Omega = \{W : \underline{w}_{ij} \leq W_{ij} \leq \bar{w}_{ij}\}, \quad (34)$$

where $\underline{w}_{ij}$ and $\bar{w}_{ij}$ are the lower and upper bounds for each element W_{ij} (i.e. row i and column j of W). Since the mandate is simple and only a few variables should be targeted, most bounds will be such that $\underline{w}_{ij} = \bar{w}_{ij} = 0$. This framework captures that the law Ω can be loose on the exact weights attached to certain variables by specifying some elements with $\underline{w}_{ij} < \bar{w}_{ij}$.

When determining the simple mandate consistent with the law Ω , we assume the central bank is benevolent and selects a weighting matrix, W^{CB*} , which minimizes the expected loss of the society. Formally,

$$W^{CB*} = \arg \min_{W \in \Omega} E \left[\left(X_t^{optimal}(W) \right)' W^{society} \left(X_t^{optimal}(W) \right) \right], \quad (35)$$

where the weighting matrix $W^{society}$ is defined by (27).

To sum up, our methodology can examine the performance of simple mandates that central banks are typically assigned with. This statement is true whether the simple mandate specifies both the target variables and the exact weights, or whether the target variables are specified but the weights are loosely defined. In this latter case, our exercise can inform central banks of the

¹⁸ Given presence of habits, there are two ways to compute CEV . One can choose whether the additional consumption units do or do not affect the habit component (lagged consumption in each period). Consistent with the convention (see e.g. Lucas, 1988, and Otrok, 2001) of increasing the steady-state consumption in all periods, our chosen measure is calibrated to the case where both current and lagged consumption is increased. It is imperative to understand that the ranking of the mandates is invariant with respect to which measure is used. The only difference between the two measures is that the other measure is 3.4125 times smaller, reflecting that accounting for the habit component requires a larger steady-state compensation. In the limit when the habit coefficient $\varkappa$ is set to unity, households would need to be compensated in terms of consumption growth.

optimal weights, and ultimately society about whether bounds on certain weights should be relaxed or not.

3. Benchmark Results

In Table 2, we report our benchmark results. The benchmark simple mandate we consider reflects the standard practice of monetary policy, and is what Svensson (2010) refers to as “flexible inflation targeting”. Specifically, we use the textbook treatment in Woodford (2003) and assume that the simple mandate can be captured by the following period loss function

$$L_t^q = (\pi_t - \pi)^2 + \lambda^q x_t^2 \quad (36)$$

where π_t denotes the quarterly inflation rate, and x_t is a measure of economic activity with λ^q denoting its corresponding weight, expressed in quarterly terms. Based on the deep parameters in his benchmark model, Woodford derives a value of 0.003 for λ^q . Most central banks, however, have a target for the annualized inflation rate. Thus, in practice the relevant weight for the measure of resource utilization is given by

$$\begin{aligned} L_t^a &= (\pi_t^a - \pi^a)^2 + \lambda^a x_t^2 \\ &= (4(\pi_t - \pi))^2 + 16\lambda^q x_t^2 = 16L_t^q \end{aligned} \quad (37)$$

where π_t^a denotes the annualized rate of quarterly inflation, and $\lambda^a (= 16\lambda^q)$ denotes the rescaled weight on economic activity taking into account that the target inflation variable is annualized. For this case, Woodford’s quarterly weight of 0.003 translates into an annualized weight of $\lambda^a = 0.048$. Throughout the paper, we will report values for λ^a .

In the first row in Table 2, we apply Woodford’s weight on three different measures of economic activity. Our first measure is the output gap. The output gap, $y_t^{gap} = y_t - y_t^{pot}$, is defined as the actual output minus the potential output that is defined as the level of output that would prevail when prices and wages are fully flexible and inefficient markup shocks are excluded.¹⁹ The second measure we consider is simply the level of output (as deviation from the deterministic labor-augmented trend, i.e. $y_t - \bar{y}_t$). Finally, we also consider annualized output growth in the spirit of the work on “speed-limit” policies by Walsh (2003).

¹⁹ We follow the terminology of Justiniano, Primiceri and Tambalotti (2013). This measure of potential output is below the efficient level (roughly by a constant amount) because we do not assume that steady-state subsidies remove the output distortion induced by the price and wage markups at the steady state. Another—perhaps more traditional—definition of potential output is based on the noninflationary maximum level of output; a popular definition by the Congressional Budget Office is based on this concept, and Plosser (2014) deals with both this concept and our welfare-relevant concept from a policy perspective.

Turning to the results in the first row we see, as expected, that adopting a target for output gap volatility yields the lowest loss; the CEV compensation for households to be indifferent is in this case nearly 4 times smaller than that required with output growth in the loss function. Another important lesson from the first row of the table is that the absolute magnitude of the CEV numbers are quite small. Only for output growth does the simple mandate generate a somewhat sizeable loss — equivalent to a compensation of 1.7 percent of steady-state consumption in every period. Given the previous literature on the welfare costs of business cycles (e.g. the seminal work by Lucas (1987) and subsequent work of Otrok (2001)), this aspect of our findings is not surprising.

Table 2: Benchmark Results for “Flexible Inflation Targeting” Mandate in eq. (37).

	x_t : Output gap		x_t : Output (dev from trend)		x_t : Output growth (Ann.)	
	λ^a	CEV (%)	λ^a	CEV (%)	λ^a	CEV (%)
Simple Mandate	0.048	0.471	0.048	0.554	0.048	0.611
Dual Mandate	0.250	0.140	0.250	0.276	0.250	0.404
Optimized Weight	1.042	0.044	0.542	0.244	2.943	0.302

Note: CEV denotes the consumption equivalent variation (in percentage points) needed to make households indifferent between the Ramsey policy and the simple mandate under consideration; see eq. (33). The “Dual Mandate” refers to a weight of unity for the unemployment gap in the loss function (37), which translates into $\lambda^a = 0.25$ when applying a variant of Okun’s law. Finally, “Optimized Weight” refers to minimization of eq. (32) w.r.t. λ^a in eq. (37).

However, the simple mandate for the U.S. Federal Reserve, the so-called dual mandate, stipulates that the Fed should jointly pursue stable prices and maximum employment. Prominent academics like Svensson (2011) have interpreted this mandate as a simple loss function in inflation and the unemployment gap (i.e. actual unemployment minus the NAIRU) where the weight placed on economic activity is substantially higher than Woodford’s (2003) value. And in recent work, Yellen (2012) and senior Federal Reserve Board staff — including Reifschneider, Wascher and Wilcox (2013) and English, Lopez-Salido and Tetlow (2013) — assigned equal weights for annualized inflation and the unemployment gap in the Federal Reserve’s loss function.

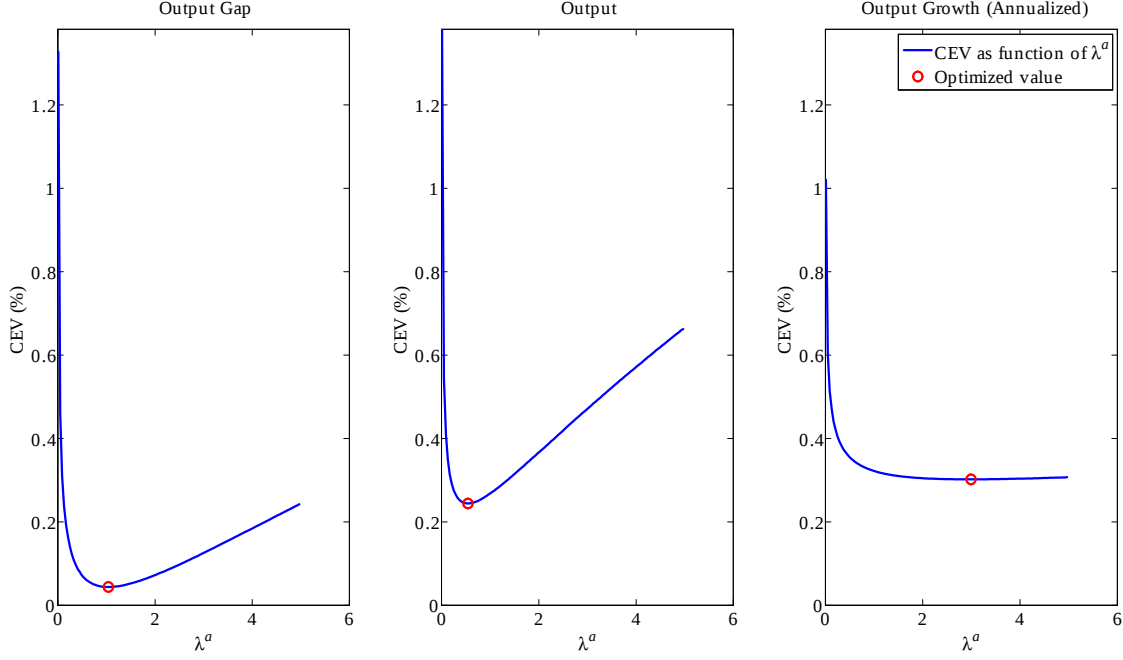
Yellen (2012) also specifies that the Federal Reserve converts the unemployment gap into an output gap according to a value of roughly 0.5. This value is based on the widely spread empirical specification of the Okun’s law:

$$u_t - u_t^{pot} = \frac{y_t - y_t^{pot}}{2}. \quad (38)$$

Accordingly, the unit weight on the unemployment gap converts into a weight of $\lambda^a = 0.25$ on the output gap when inflation is annualized.²⁰ This value is roughly five times bigger than the value

²⁰ Moreover, Gali, Smets and Wouters (2011) argue within a variant of the SW model with unemployment that fluctuations in their estimated output gap closely mirror those experienced by the unemployment rate. Therefore, the Okun’s law we apply can also find support in a structural modeling framework.

Figure 1: Consumption Equivalent Variation (percentage points) as Function of the Weight (λ^a) on Economic Activity.



derived by Woodford, and indicates a lack of consensus regarding the weight that real activity should receive.

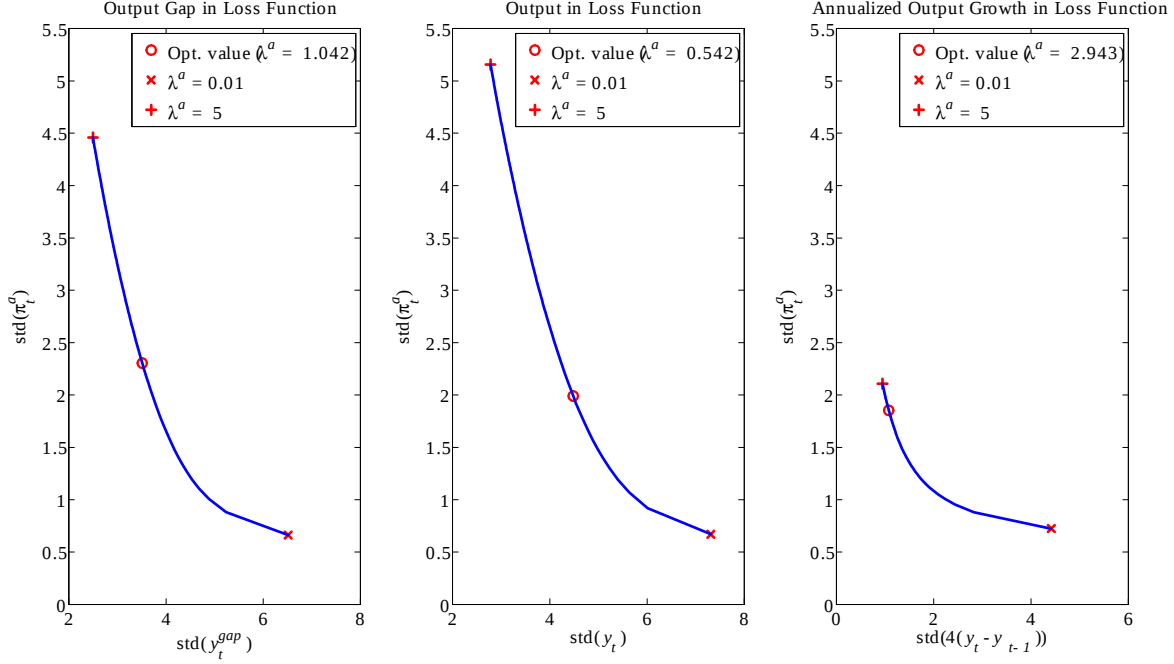
Interestingly, we can see from the second row in Table 2 that increasing the weight on real activity from Woodford's to the value consistent with the "Dual Mandate" reduces welfare losses by a factor of two in the cases of output and output growth. For the more standard measure of the output gap, the losses under the dual mandate are more than three times smaller. The third row in Table 2 displays the results when the weight λ^a is optimized ("Optimized Weights"). The optimized coefficient for the output gap is 1.042—much higher than in the two preceding loss functions. When the level of output replaces the output gap, the optimized coefficient is about 0.5. In the case of output growth, the optimized coefficient is even higher (2.9), which is essentially a so-called speed-limit regime (see Walsh, 2003). Responding to the model-consistent output gap is the preferred measure from a welfare perspective, but our analysis suggests that a large weight should be assigned to stabilize economic activity in addition to inflation regardless of the chosen resource utilization measure.

To get a better sense of the curvature of the CEV with respect to the weight assigned to resource utilization, Figure 1 plots the CEV as function of λ^a for the three resource measures. Consistent with the results in Table 2, we see that there is quite some curvature of the CEV function for small values of λ^a for all three measures. Moreover, for the output gap we see that values between 0.5 and 1.5 perform about equally well, whereas the range for λ^a where output performs about the same is rather narrow. For output growth, the figure shows that any value above unity yields about the same CEV. As noted in Section 2.2, all our results are based on a non-efficient steady state. Our results in Table 2 and Figure 1, however, are robust to allowing for subsidies to undo the steady-state distortions stemming from firms' and households' monopoly power in price and wage setting. For the output gap and output as deviation from its trend, the optimized λ^a is roughly unchanged; but for output growth, our optimized λ^a is substantially lower (0.43). Given the flatness of the CEV function in Figure 1, it is not surprising that the results for output growth can be somewhat sensitive to the specific assumptions. Even so, the optimized weight on resource utilization is still relatively large, reflecting the larger curvature for smaller values of λ^a .

To understand the curvature of the CEV for the various resource utilization measures in Figure 1, it is useful to depict variance frontiers. We do this in Figure 2. In the figure, the blue line shows the combination of inflation-resource utilization volatility when λ^a varies from 0.01 to 5. The coordinate with an 'x' mark shows the volatility for $\lambda^a = 0.01$, the 'o' mark shows the volatility for the optimized weight, and the '+' mark shows the volatility for $\lambda^a = 5$. The figure shows that the trade-off between stabilizing inflation and economic activity is more favorable when the resource utilization measure is output growth (right panel); the standard deviation of annualized output growth can be reduced to about 2 percent before $\text{std}(\pi_t^a)$ exceeds unity. Because inflation volatility is so little affected when λ^a is increased, it is not surprising that the optimized λ^a is relatively high. Moreover, the flatness of the CEV witnessed in the right panel of Figure 1 for $\lambda^a > 2.943$ can be readily explained by the fact that Figure 2 shows that such values induce only small changes in inflation volatility. Turning back to the results for output and the output gap, the figure shows that the trade-off is more pronounced, especially for output (as deviation from trend, middle panel). Accordingly, the optimized values for λ^a are lower and the CEV curvature is substantial in Figure 1 for higher values of λ^a .

Apart from helping to explain the optimized values in Table 2, another key feature of Figure 2 is the important trade-off between stabilizing inflation and the output gap in the SW model. This finding is seemingly at odds with Justiniano, Primiceri and Tambalotti (2013) who argue that there

Figure 2: Variance Frontier for Alternative Resource Utilization Measures.



is little evidence that stabilizing the output gap comes at the price of higher inflation volatility. In the next section we address this issue together with the reasons for the importance of real activity.

3.1. The Importance of Real Activity

The key message from Table 2 is that the rationale for targeting some measure of real activity is much more important than previously thought either in policy circles or in previous influential academic work (e.g. Woodford (2003) and Walsh (2005)). By perturbing the parameter values (i.e. turning off some bells and whistles) in the model, we seek to nail down why the model suggests that a high weight on real economic volatility improves household welfare.

We begin the analysis by using the SW parameters in Table 1 to recompute λ^a according to the analytic formula provided in Woodford (2003):

$$\lambda^a \equiv \frac{16\kappa_x}{\left(\frac{\phi_p}{\phi_p - 1}\right)}, \quad (39)$$

where κ_x is the coefficient for the output gap in the linearized pricing schedule (i.e. in the New Keynesian Phillips curve), and $\frac{\phi_p}{\phi_p - 1}$ is the elasticity of demand of intermediate goods. In the SW

model, the NKPC is given by

$$\pi_t - \iota_p \pi_{t-1} = \beta \gamma^{1-\sigma_c} (E_t \pi_{t+1} - \iota_p \pi_t) + \frac{(1 - \beta \gamma^{1-\sigma_c} \xi_p) (1 - \xi_p)}{\xi_p ((\phi_p - 1) \epsilon_p + 1)} mc_t + \varepsilon_{p,t}. \quad (40)$$

However, because the SW model features endogenous capital and sticky wages, there is no simple mapping between the output gap and real marginal costs within the fully fledged model. But by dropping capital and the assumption of nominal wage stickiness, we can derive a value of $\kappa_x = 0.143$ in the (simplified) SW model.²¹ From the estimated average mark-up ϕ_p , we then compute $\lambda^a = 0.87$. This value is considerably higher than Woodford’s (2003) value of 0.048 for two reasons. First, Woodford’s κ_x is substantially lower due to the assumption of firm-specific labor (the Yeoman-farmer model of Rotemberg and Woodford, 1997). Second, the estimated mark-up in SW implies a substantially lower substitution elasticity ($\frac{\phi_p}{\phi_p - 1} = 2.64$) compared to Woodford’s value (7.88).

We caution that this analysis is only tentative, as it by necessity only considers a simplified model without some of the key features in the fully fledged model. As a consequence, the obtained λ^a will only partially reflect the true structure of the fully fledged SW model. Yet, the analysis suggests that a large part of the gap between Woodford’s (2003) value and our benchmark finding of $\lambda^a = 1.042$ in the output-gap case stems from differences in household preferences and the estimated substitution elasticity between intermediate goods.

After this initial exercise, we turn to exploring the mechanisms within the context of the fully fledged model. Our approach is to turn off or reduce some of the frictions and shocks featured in the model one at a time to isolate the drivers of our results. The findings are provided in Table 3. In the table, the first row restates our benchmark value of λ^a , i.e. the “Optimized Weight” row of Table 2 which is based on the benchmark calibration of the model. The second row, denoted as “No Indexation,” presents the optimized weight on the real-activity term when dynamic indexation in price- and wage-setting is shut down, i.e. ι_p and ι_w are calibrated to zero. All the other parameters of the model are kept unchanged. As can be seen from the table, the “No Indexation” calibration lowers the optimized weight for the output gap to roughly 0.3—about a third of the benchmark value. In the other columns where real activities are captured by the level and the growth rate of detrended output, the optimized weights are also found to be about a third of the benchmark values.

²¹ More specifically, we derive $\pi_t - \iota_p \pi_{t-1} = \beta \gamma^{1-\sigma_c} (E_t \pi_{t+1} - \iota_p \pi_t) + \kappa_x \left[x_t - \frac{\kappa}{1 + \sigma_l (1 - \kappa)} x_{t-1} \right] + \varepsilon_{p,t}$ where x_t is the output gap and the slope coefficient κ_x equals $\frac{(1 - \beta \gamma^{1-\sigma_c} \xi_p) (1 - \xi_p)}{\xi_p ((\phi_p - 1) \epsilon_p + 1)} \left(\frac{1 + \sigma_l (1 - \kappa)}{1 - \kappa} \right)$.

Table 3: Perturbations of the Benchmark Model.

	x_t : Output gap		x_t : Output (dev from trend)		x_t : Output growth (Ann.)	
Simple Mandate	λ^a	CEV (%)	λ^a	CEV (%)	λ^a	CEV (%)
Benchmark	1.042	0.044	0.542	0.244	2.943	0.302
No Indexation	0.318	0.042	0.179	0.220	0.817	0.285
No ε_t^p Shocks	0.914	0.039	0.343	0.220	1.235	0.278
No ε_t^w Shocks	2.094	0.020	0.355	0.213	1.267	0.226
Small ε_t^p and ε_t^w Shocks	1.268	0.024	0.112	0.167	0.157	0.180
No ε_t^p and ε_t^w Shocks	Large	0.016	0.161	0.150	0.025	0.134

Note: “No Indexation” refers to setting $\iota_p = \iota_w = 0$; “No ε_t^p (ε_t^w) Shocks” refers to setting the variance of the price markup shock (wage markup shock) to zero; “Small ε_t^w and ε_t^p Shocks” means that the std of these shocks are set to a 1/3 of their baseline values; and “No ε_t^w and ε_t^p Shocks” refers to setting the variance of both shocks to zero. “Large” means that the optimized value is equal or greater than 5.

To understand why indexation makes the real-activity term much more important than in a model without indexation, it is instructive to consider a simple New Keynesian model with indexation and sticky prices only. If we compute a micro-founded welfare-based approximation to the household utility function following Woodford (2003), such a model would feature the following terms in the approximated loss function

$$(\pi_t - \iota_p \pi_{t-1})^2 + \lambda (y_t^{gap})^2, \quad (41)$$

where ι_p is the indexation parameter in the pricing equation. Suppose further, for simplicity, that inflation dynamics in equilibrium can be represented by an AR(1) process $\pi_t = \rho \pi_{t-1} + \varepsilon_t$. In this simple setup, the welfare metric could be expressed as follows:

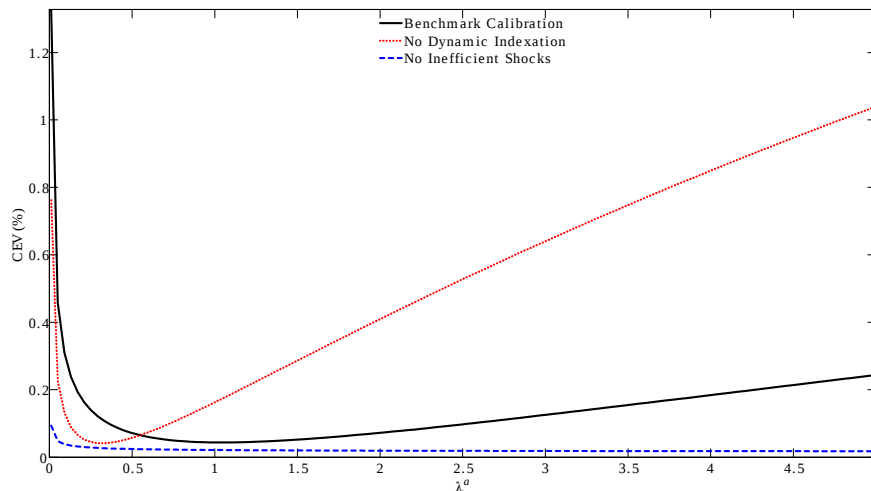
$$\mathbb{E}_0 \left[(\rho - \iota_p)^2 (\pi_{t-1})^2 + \lambda (y_t^{gap})^2 \right]. \quad (42)$$

Intuitively, in economies where prices have a component indexed to their lags, inflation does not create any much price distortions. Consequently, there is less need to stabilize it.

In more empirically relevant models like SW, inflation persistence (ρ) is in large part explained by the indexation parameter (ι_p). Therefore, these two parameter values tend to be similar and the coefficient in front of the inflation term is accordingly smaller. Hence, in a loss function like ours (eq. 37) where the inflation coefficient is normalized to unity, the coefficient in front of real activity tends to become relatively larger—as evidenced in Table 2.

Notably, even when we take out price and wage indexation, the optimal value for λ^a still suggests a very large role for targeting economic activity; in fact, it is even slightly higher than the value implied by the dual mandate. Moreover, we see from Figure 3 that dropping dynamic indexation is associated with a rather sharp deterioration in the CEV when λ^a is below 0.2. This finding suggests that a vigorous response to economic activity is indeed important even without indexation.

Figure 3: CEV (in percentage points) as Function of λ^a for Alternative Calibrations.



Additionally, it is also important to point out that we kept all other parameters unchanged in this analysis; had we reestimated the model it is conceivable that the other parameters would change as to better account for the high degree of inflation persistence prevailing in the data, and accordingly again implied a higher λ^a .²²

Rows 3–6 in Table 3 examine the role of the inefficient “markup” shocks in the model. By comparing the CEV results in the third and fourth rows, we see that the wage markup shock contributes the most to the welfare costs of the simple mandate. But the key point is that even when one of these shocks is taken out of the model, the CB should still respond vigorously to economic activity in order to maximize welfare of the households inhabiting the economy. Only when the standard deviation of both shocks are reduced or taken out completely (rows 5 and 6), λ^a falls sharply for output and output growth. For the loss function with the model-consistent output gap, the weight λ^a becomes very hard to pin down numerically when the standard deviation of both the inefficient shocks are set to nil because any $\lambda^a > 0.1$ produces roughly the same CEV of about 0.016 although a $\lambda^a \geq 5$ generates the lowest welfare loss relative to Ramsey as can be seen from Figure 3, which plots CEV as function of λ^a for some alternative calibrations of the model. So in the absense of price- and wage-markup shocks, this finding suggests that there is only a weak trade-off between inflation stabilization and stabilization of the output gap. Even so, the “divine coincidence” feature noted by Blanchard and Galí (2007) only holds approximately as the

²² Excluding indexation to lagged inflation in price and wage setting is associated with a deterioration in the empirical fit (i.e. reduction in marginal likelihood) of the model.

SW model features capital formation and sticky wages; see Woodford (2003) and Galí (2008).

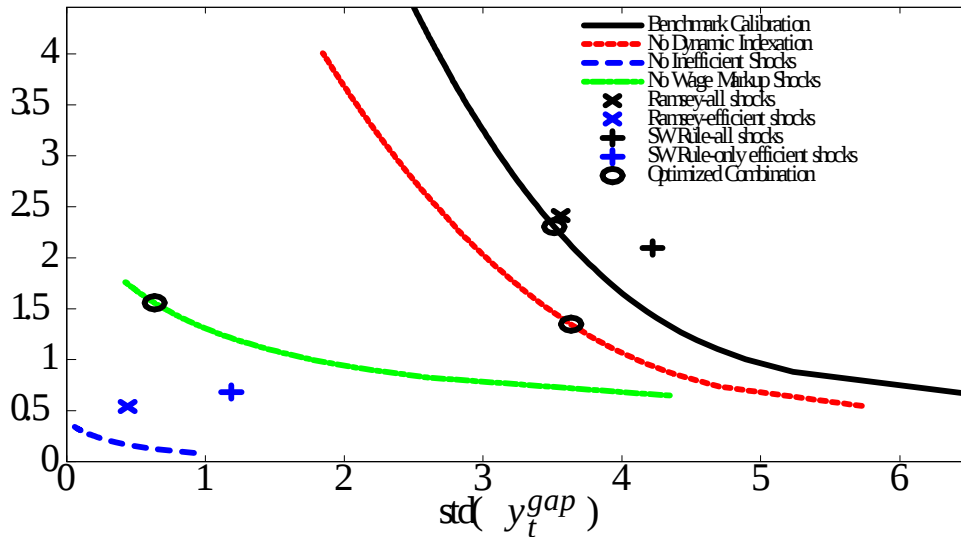
A traditional way to represent a possible trade-off between inflation and output stabilization is through variance frontiers. In Figure 4, we depict variance frontiers when varying λ^a from 0.01 to 5 for alternative calibrations of the model. We also include the implied $\{\text{std}(\pi_t^a), \text{std}(y_t^{gap})\}$ combinations under Ramsey policy and the estimated SW policy rule with all shocks (marked by black ‘x’ marks) and without the inefficient shocks (the blue ‘+’ marks). As expected, we find that both the estimated rule and the Ramsey policy is outside the variance frontier associated with the simple mandate (solid black line), but that the locus of $\{\text{std}(\pi_t^a), \text{std}(y_t^{gap})\}$ for the optimized λ^a for the simple mandate is very close to the Ramsey policy.

From the figure, we also see that omitting dynamic indexation shifts the variance frontier inwards; however, there is still a substantial trade-off between inflation and output gap stabilization, as the central bank has to accept a higher degree of inflation volatility when increasing the weight (λ^a) on output gap stabilization. Interestingly, we see that the optimized λ^a in the no-dynamic indexation case is associated with slightly higher output volatility and lower inflation volatility relative to the benchmark calibration. This is because when none of the non-optimizing firms and households index their prices and wages to the lagged inflation rate, it becomes more costly to allow inflation to fluctuate from its steady state which is then the rate of inflation all non-optimizing agents would use in indexing their prices and wages.

Further, there is a noticeable trade-off between inflation and output gap volatility even when we follow Justiniano, Primiceri and Tambalotti (2013) and set the standard deviation of the “wage markup” shocks to nil (dash-dotted green line). The reason why the central bank has to accept a higher degree of inflation volatility in order to reduce output gap volatility in this case is that we still have the “price markup” shock active in the model. When the inefficient price markup shocks are excluded as well (dashed blue line in Figure 4), there is only a very moderate inflation-output volatility trade-off. In this special case, we also reproduce the key finding in Justiniano, Primiceri and Tambalotti (2013); namely that a shift from the estimated historical rule to Ramsey policy is a free lunch as it reduces output gap volatility without the expense of higher inflation volatility.²³ Notably, this result does not arise in the case when both types of inefficient markup shocks are included; in this case, a shift from the estimated rule to Ramsey policy will be associated with a decline in output gap volatility but rising inflation volatility.

²³ To account for inflation persistence without correlated price markup shocks, Justiniano, Primiceri and Tambalotti (2013) allow for serially correlated shocks to the Fed’s inflation target which are subsequently excluded in their optimal policy exercises.

Figure 4: Variance Frontiers for Alternative Calibrations.



It is important to note that even the model variant without the inefficient shocks—which features only a modest trade-off between stabilizing inflation and the output gap as in Justiniano, Primiceri and Tambalotti (2013)—warrants a relatively high λ^a (although the choice of λ^a will be less important from a welfare point of view). Table 3 and Figure 3 document that, absent the inefficient markup shocks, a value for λ^a above 0.1 is nevertheless warranted. Moreover, in the more likely case where indeed at least a small proportion of the observed variation in inflation and wages are in fact driven by inefficient price- and wage-markup shocks, the optimal value of λ^a should not only be high but also matter importantly for the inflation-output gap trade-off (in line with our results for the benchmark calibration). The fifth row in Table 3 makes this point by reporting results where the standard deviations of the inefficient markup shocks have been set to a third of their baseline values. From the table, we see that the resulting λ^a is still high for the output gap; in fact, it is higher than our baseline value.

4. Robustness Analysis

In this section, we explore the robustness of our results along some key dimensions. We first examine to what extent adding labor market variables like hours worked and wage inflation to the loss function improves welfare. Second, we consider the merits of so-called speed limit policies analyzed by Walsh (2003) and price- and wage-level targeting. Third and finally, we consider the extent to which the implied interest rate movements for the simple mandates under consideration

are reasonable.

4.1. A Quest for a Different Objective: Should Labor Market Variables be considered?

One of the reasons for the popularity of inflation targeting comes from the results in the New Keynesian literature—importantly Clarida, Gali and Gertler (1999) and Woodford (2003)—that inflation in the general price level is costly to the economy. The old Keynesian literature, however, emphasized the importance of wage inflation.²⁴ Recent influential theoretical papers support that literature by suggesting to add wage inflation as an additional target variable, see e.g. Erceg, Henderson and Levin (2000) and Gali (2011). In the SW model employed in our analysis, both nominal wages and prices are sticky. It is therefore conceivable that wage inflation may be equally or even more important to stabilize than price inflation. In addition to studying nominal wage inflation, it is of interest to examine to what extent other labor market variables like hours worked can substitute for overall economic activity within the model. Hence, we propose to study the following augmented loss function:

$$L_t^a = \lambda_\pi^a (\pi_t^a - \pi^a)^2 + \lambda^a x_t^2 + \lambda_{\Delta w}^a (\Delta w_t^a - \Delta w^a)^2 + \lambda_e^a e_t^2, \quad (43)$$

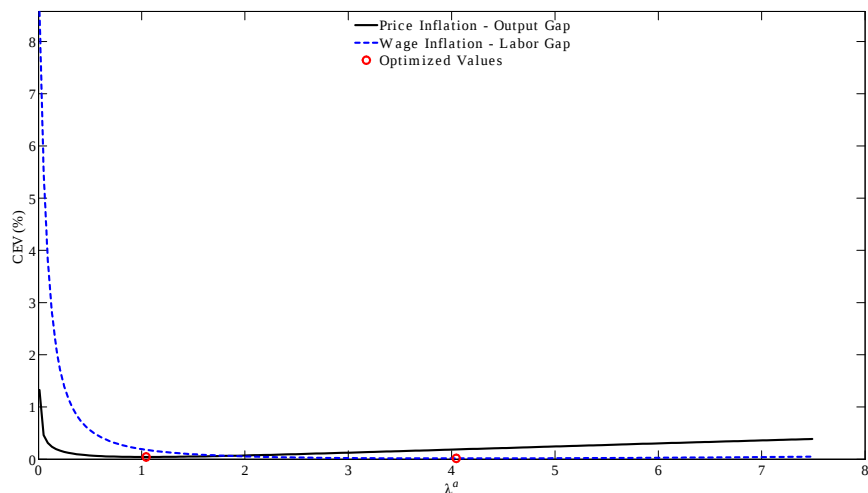
where Δw_t^a denotes annualized wage inflation, x_t is—as before—a measure of overall economic activity, and e_t is a measure of activity in the labor market.

In Table 4, we report results for this augmented loss function (43) when x_t is given by the output gap and l_t is given by the hours worked per capita gap, respectively. The first row re-states the benchmark results, i.e. the “Optimized Weight” coefficient for y_t^{gap} in Table 2. The second row adds wage inflation to the loss function. Relative to the unit weight on inflation, the optimized objective function would ask for a weight of roughly 3.2 for the output gap term, and a weight of about 1.5 for wage inflation volatility, which is higher than the normalized weight on price inflation volatility. The level of welfare is also substantially higher (by 32.8 percent, when measured by the decrease in loss) than under the benchmark case. However, responding to price inflation is still sizeably welfare enhancing, a feature we learn from the third row in the table where Δw_t replaces π_t ; in this case the welfare gain is somewhat lower compared to the trivariate loss function.

Next, we introduce the labor market gap, defined as $l_t^{gap} = l_t - l_t^{pot}$, as an additional target variable in the fourth column of Table 4. Unlike wage inflation, the inclusion of the labor market gap by itself does not increase welfare much. Moreover, given that price inflation is the nominal

²⁴See Kim and Henderson (2005) for a more detailed discussion and references.

Figure 5: CEV (in percentage points) as Function of λ^a for Alternative Simple Mandates.



anchor, replacing the output gap with the labor gap results in a welfare deterioration of about 14 percent relative to our benchmark specification as can be seen from the fifth row. However, when price inflation is also replaced by wage inflation as a target variable, the labor gap performs much better, and this labor market oriented simple mandate generates a substantial welfare gain of 63 percent relative to our benchmark specification.

In Figure 5, we plot CEV as a function of λ^a for the simple mandate targeting price inflation and the output gap as well as the mandate targeting wage inflation and the labor market gap. Interestingly, we see from the figure that λ^a has to exceed 2 in order for the wage-labor simple mandate to dominate. So although the wage-labor gap mandate dominates the inflation-output gap mandate, the figure makes clear that a rather large λ^a is required for this to happen; strict nominal wage inflation targeting is thus very costly for society in terms of welfare. On the other hand, a beneficial aspect of the wage inflation-labor gap is that if λ^a indeed exceeds this threshold, then the CEV stays essentially flat instead of increasing as is the case for the inflation-output gap mandate.

Table 4: Variations of the Loss Function: Gap Variables in (43).

Loss Function	$\lambda_\pi^a: \pi_t^a$	$\lambda^a: y_t^{gap}$	$\lambda_w^a: \Delta w_t$	$\lambda_e^a: l_t^{gap}$	CEV (%)	Gain
Benchmark	1.000	1.042	—	—	0.044	—
Adding Δw_t	1.000	3.216	1.485	—	0.029	32.8%
Replacing π_t with Δw_t	—	1.546	1.000	—	0.032	27.3%
Adding l_t^{gap}	1.000	0.880	—	0.518	0.043	1.6%
Replacing y_t^{gap} with l_t^{gap}	1.000	—	—	3.250	0.050	−14.3%
Replacing $[\pi_t, y_t^{gap}]$ with $[\Delta w_t, l_t^{gap}]$	—	—	1.000	4.044	0.016	63.3%

Note: The table reports variations of the simple objective (43). y_t^{gap} is used as measure for x_t , and l_t^{gap} is used as measure of e_t . The numbers in the “Gain” column are computed as $100 \left(1 - \frac{CEV_{LFalt}}{0.0437}\right)$ where CEV_{LFalt} is the CEV for the alternative loss function and 0.0437 is the “Benchmark” objective CEV (row 1).

We also examine the role of labor market variables when only observable variables are included; hence, we consider levels instead of gap variables. As shown in Table 5, the role played by nominal wage inflation is not as prominent when x_t in (43) is represented by the level of output (as deviation from trend) instead of the output gap. The welfare gain relative to the benchmark case is only 5.3 percent higher when wage inflation is included in (43). Accordingly, welfare is reduced by one percent—the third row—when price inflation is omitted. On the other hand, adding hours worked per capita enhances the welfare of households by nearly 30 percent. Finally, we see from the last row that a mandate with only wage inflation and hours worked performs the best, and reduces the welfare cost associated with the simple mandate by nearly 34 percent relative to the benchmark objective.

Table 5: Variations of the Loss Function: Level Variables in (43).

Loss Function	$\lambda_\pi^a: \pi_t^a$	$\lambda^a: y_t - \bar{y}_t$	$\lambda_w^a: \Delta w_t$	$\lambda_e^a: l_t - \bar{l}$	CEV (%)	Gain
Benchmark	1.000	0.544	—	—	0.244	—
Adding Δw_t	1.000	0.954	0.463	—	0.230	5.3%
Replacing π_t with Δw_t	—	1.054	1.000	—	0.246	−1.0%
Adding $l_t - \bar{l}$	1.000	0.392	—	1.344	0.171	29.8%
Replacing $y_t - \bar{y}_t$ with $l_t - \bar{l}$	1.000	—	—	2.947	0.210	13.8%
Replacing $[\pi_t, y_t - \bar{y}_t]$ with $[\Delta w_t, l_t - \bar{l}]$	—	—	1.000	3.475	0.161	33.8%

Note: The table reports variations of the simple objective (43). $y_t - \bar{y}_t$ is used as measure for x_t , and $l_t - \bar{l}$ is used as measure of e_t . The numbers in the “Gain” column are computed as $100 \left(1 - \frac{CEV_{LFalt}}{0.2440}\right)$ where CEV_{LFalt} is the CEV for the alternative loss function and 0.2440 is the “Benchmark” objective CEV (row 1).

Our conclusion is that while a standard objective with price inflation and the output gap generates small welfare losses relative to Ramsey policy (around 0.03% of steady state consumption), it makes sense within the SW model—which features substantial frictions in the labor market—to target wage inflation and a labor market gap instead. Doing so will reduce the welfare costs of the simple mandate even further. Moreover, we have shown that this conclusion is robust even if one considers the level of output and hours worked instead of their deviations around potential.

Furthermore, regardless of whether the objective focuses on price or wage inflation, we always find a robust role for responding vigorously to economic activity (may it be output or hours worked), in line with our benchmark results in Table 2.

4.2. Another Quest for a Different Objective: Speed Limit Policies & Price- and Wage-Level Targeting

In this subsection, we examine the performance of so-called speed limit policies (SLP henceforth) advocated by Walsh (2003) and price- and wage-level targeting.

We start with an analysis of SLP. Walsh’s formulation of SLP considered actual growth relative to potential (i.e. output gap growth), but we also report results for actual growth relative to steady state to understand how contingent the results are on measuring the change in potential accurately. Moreover, since the results in the previous subsection suggested that simple mandates based on the labor market performed very well, we also study the performance of SLP for a labor market based simple mandate.

We report results for two parameterizations of the SLP objective in Table 6.a. In the first row, we use the benchmark weight derived in Woodford (2003). In the second row, we use a weight that is optimized to maximize household welfare. Interestingly, we see that when replacing the level of output growth with the growth rate of the output gap (Δy_t^{gap}), welfare is increased substantially conditional on placing a sufficiently large coefficient on this variable. However, by comparing these results with those for y_t^{gap} in Table 2, we find it is still better to target the level of the output gap.

Turning to the objectives based on nominal wage inflation and hours, we see that they perform less well than the standard inflation-output objectives unless the weight on the labor gap is sufficiently large. As is the case for output, the growth rate of the labor gap is preferable to the growth rate of labor itself. But by comparing with our findings in Table 4 we see that targeting the level of the labor gap is still highly preferable in terms of maximizing welfare of the households.

Table 6.a: Sensitivity Analysis: Merits of Speed Limit Policies.

Parameterization	Price Inflation Objective				Wage Inflation Objective			
	$x_t: \Delta y_t$		$x_t: \Delta y_t^{gap}$		$x_t: \Delta l_t$		$x_t: \Delta l_t^{gap}$	
	λ^a	CEV (%)	λ^a	CEV (%)	λ^a	CEV (%)	λ^a	CEV (%)
Woodford	0.048	0.611	0.048	0.525	0.048	0.885	0.048	0.817
Optimized	2.943	0.302	11.21	0.079	18.60	0.212	21.68	0.058

Note: The loss function under price inflation is specified as in (37), while the loss function with the annualized nominal wage inflation rate wage is specified as $(\Delta w_t^a - \Delta w^a)^2 + \lambda^a x_t^2$. Δy_t denotes annualized output growth as deviation from the s.s. annualized growth rate $(4(\gamma - 1))$. Δy_t^{gap} is the annualized rate of growth of output as

deviation from potential, i.e. $4(\Delta y_t - \Delta y_t^{pot})$. The same definitions apply to hours worked. See notes to Table 2 for further explanations.

Several important papers in the previous literature have stressed the merits of price level targeting as opposed to the standard inflation targeting loss function (see e.g. Vestin, 2006)). Price level targeting is a commitment to eventually bring back the price level to a baseline path in the face of shocks that creates a trade-off between stabilizing inflation and economic activity. Our benchmark flexible inflation targeting objective in eq. (37) can be replaced with a price level targeting objective as follows:

$$L_t^a = (p_t - \bar{p}_t)^2 + \lambda^a x_t^2, \quad (44)$$

where p_t is the actual log-price level in the economy and $\bar{p}_t$ is the target log-price level path which grows with the steady state net inflation rate π according to $\bar{p}_t = \pi + \bar{p}_{t-1}$. When we consider wage level targeting we adopt a specification isomorphic to that in (44), but replace the first term with $w_t - \bar{w}_t$ where w_t is the nominal actual log-wage and $\bar{w}_t$ is the nominal target log-wage which grows according to $\bar{w}_t = \ln(\gamma) + \pi + \bar{w}_{t-1}$ where γ is the gross technology growth rate of the economy (see Table 1).

In Table 6.b, we report results for both price- and wage-level targeting objectives. As can be seen from the table, there are no welfare gains from pursuing price-level targeting relative to our benchmark objective in Table 2 (which yielded a CEV of 0.0437 for the price-inflation output-gap specification), regardless of whether one targets the output or the hours gap. For wage-level targeting, we obtain the same finding (in this case, the relevant comparison is the wage-inflation hours-gap specification in Table 4 which yields a CEV of 0.0160). These findings are perhaps unsurprising, given that the welfare costs in our model are more associated with changes in prices and wages (because of indexation) than with accumulated price- and wage-inflation rates.

Table 6.b: Sensitivity Analysis: Merits of Price and Wage Level Targeting.

Parameterization	Price-Level Targeting				Wage-Level Targeting			
	$x_t: y_t^{gap}$		$x_t: l_t^{gap}$		$x_t: y_t^{gap}$		$x_t: l_t^{gap}$	
	λ^a	CEV (%)	λ^a	CEV (%)	λ^a	CEV (%)	λ^a	CEV (%)
Woodford	0.048	0.542	0.048	0.776	0.048	0.502	0.048	0.688
Optimized	9.187	0.092	28.41	0.095	11.37	0.064	36.14	0.067

Note: The loss function under price-level targeting is given by (44), while the loss function with the nominal wage level is specified as $L_t^a = (w_t - \bar{w}_t)^2 + \lambda^a x_t^2$. See notes to Table 2 for further explanations.

4.3. Concerns on the Volatility of Interest Rates

In addition to inflation and some measure of resource utilization, simple objectives often include a term involving the volatility of interest rates; see e.g. Rudebusch and Svensson (1999). In practice, this term is often motivated by reference to “aversion to interest-rate variability” and financial stability concerns. From a theoretical perspective, Woodford (2003) derives an extended version of (37) augmented with an interest rate gap term $\lambda_r (r_t^a - r^a)^2$ when allowing for monetary transactions frictions ($r_t^a - r^a$ is the deviation of the annualized nominal policy rate r_t^a around the steady state annualized policy rate r^a).

As an alternative, some researchers (e.g. Rudebusch and Svensson, 1999) and policymakers (e.g. Yellen, 2012) instead consider augmenting the objective function with the variance of the *change* in the short-run interest rate, i.e. $\lambda_r (\Delta r_t^a)^2$. By allowing for a lag of the interest rate in the loss function, the specification introduces interest rate smoothing, as the reduced-form solution will feature the lagged interest rate in the central banks reaction function. Both specifications, however, will reduce volatility of policy rates because the central bank will, *ceteris paribus*, tend to be less aggressive in the conduct of monetary policy when $\lambda_r > 0$.

The first row in Table 7 considers the standard Woodford (2003) specification with only x_t as an additional variable to inflation as in (37). The second row in the table includes the $(r_t^a - r^a)^2$ term in the loss function and uses Woodford’s (2003) weights for economic activity and the interest rate (0.048 and 0.077, respectively). The third row reports results for Yellen’s (2012) specification of the loss function which includes the $(\Delta r_t^a)^2$ term in the loss function instead of $(r_t^a - r^a)^2$ and uses her weights (0.25 and 1.00, respectively). Finally, the last two rows present results when the coefficient on x_t and the interest rate gap—row 4—and the change in the interest rate gap—row 5—are optimized to maximize welfare of the households.

Turning to the results, we see by comparing the first and second rows in the table that the CEV is not much affected by the introduction of the interest term for the output gap and output. For output growth, however, including the interest rate term reduces the welfare costs by more than a factor of 2. Comparing the third row—the Yellen parameterization—with the Woodford specification in the second row, we see that while welfare improves considerably for all three different x_t variables, it is only for output growth that this improvement stems from the interest rate term. For the output gap and output, the improvement is mostly due to the higher λ^a , which can be confirmed by comparing the “Dual Mandate” row in Table 2 with the Yellen row in Table 7.

When allowing for optimal weights (the last two rows in Table 7), we find that the optimized weight on the interest rate term in both cases are driven towards zero for the output gap, implying that the welfare consequences are marginal. Only for output and output growth do we find modest welfare improvements from including any of the two interest rate terms (compared to our benchmark results in Table 2 where CEV equaled 0.2440 and 0.3020 for output and output growth, respectively). However, in all cases our key finding holds up—some measure of real activity should carry a large weight.

Table 7: Sensitivity Analysis: Minimization of (37) with an interest rate term.

Loss Function	x_t : Output Gap			x_t : Output (dev from trend)			x_t : Output Growth (Ann.)		
	λ^a	λ_r	CEV (%)	λ^a	λ_r	CEV (%)	λ^a	λ_r	CEV (%)
Woodford: only x_t	0.048	—	0.471	0.048	—	0.554	0.048	—	0.611
Woodford: $r_t^a - r^a$	0.048	0.0770	0.462	0.048	0.0770	0.452	0.048	0.0770	0.523
Yellen: Δr_t^a	0.250	1.0000	0.186	0.250	1.0000	0.242	0.250	1.0000	0.547
Optimized: $r_t^a - r^a$	1.042	0.0001	0.044	0.461	0.1067	0.215	2.364	0.0926	0.280
Optimized: Δr_t^a	1.042	0.0001	0.044	0.530	0.0261	0.216	2.700	0.0827	0.285

Note: The loss function with the level of the interest rate is specified as $(\pi_t^a - \pi^a)^2 + \lambda^a x_t^2 + \lambda_r (r_t^a - r^a)^2$, while the loss function with the change in the interest rate is specified as $(\pi_t^a - \pi^a)^2 + \lambda^a x_t^2 + \lambda_r (\Delta r_t^a)^2$. See notes to Table 2 for further explanations.

One of the concerns for financial stability is that the nominal interest rate is conventionally the key instrument of monetary policy. In this vein, high volatility of interest rates could be problematic for financial markets if such policies were implemented. An additional concern is whether the probability distribution of nominal rates for the mandates under consideration covers the negative range in a nontrivial way. One of the advantages of specifying a simple mandate, rather than a simple interest rate rule, is that the central bank can choose to use a variety of instruments to implement the desired objective. Besides nominal interest rates, such instruments can include forward guidance, reserve requirements, asset purchases, money instruments and others. So even though the zero lower bound on nominal interest rates *per se* is less of a concern in our analysis, we still want examine to what extent our results are robust to limiting the short-term variability of monetary policy.

In what follows, we use a standard approach to limit the standard deviation of the nominal interest rate: Rotemberg and Woodford (1998) adopts the rule of thumb that the steady-state nominal rate minus two standard deviations (std) for the rate should be non-negative. Others, like Adolfson et al. (2011) have adopted a three std non-negativity constraint. Since our adopted parameterization of the SW model implies an annualized nominal interest rate of 6.25 percent, the allowable std is 3.125 under the Rotemberg and Woodford’s rule of thumb and slightly below 2.1

under the stricter three-std criterion adopted by Adolfson et al. (2011). So although inclusion of $r_t^a - r^a$ or Δr_t^a does not improve welfare much, we are interested in examining to what extent our optimized simple mandates without interest rate terms are associated with excessive interest rate volatility and to what extent including the interest rate terms mitigates such excessive volatility.

Table 8 reports the result of our exercise. For brevity of exposition we focus on the output gap only, but the results are very similar for output level and output growth. As seen from the first three rows in the table, the objective functions in Table 2 that involve only inflation and the output gap are indeed associated with high interest rate volatility. The std's are all around 9 percentage points – a few times bigger than our thresholds. Hence, these loss functions are contingent on unrealistically large movements in the short-term policy rate. Turning to the fourth and fifth rows, which report results for the Woodford and Yellen loss functions augmented with interest rate terms, we see that the std's for the policy rate shrink by almost a factor of ten; these specifications are hence clearly consistent with reasonable movements in the stance of monetary policy.

Table 8: Interest Rate Volatility for Output Gap in Loss Function.

Loss Function	λ^a	λ_r	CEV (%)	$\text{std}(r_t^a)$
Woodford	0.048	—	0.471	8.92
Dual Mandate	0.250	—	0.140	8.76
Optimized	1.042	—	0.044	9.00
Woodford: $r_t^a - r^a$	0.048	0.0770	0.462	0.98
Yellen: Δr_t^a	0.250	1.0000	0.186	1.24
Optimized*: $r_t^a - r^a$	1.161	0.0770*	0.076	2.24
Optimized*: Δr_t^a	1.110	1.0000*	0.084	2.04

Note: $\text{std}(r_t^a)$ denotes the standard deviation for the annualized nominal interest rate. y_t^{gap} is used as measure of x_t in the loss function. The * in the last two rows denote that these values have been fixed, and are hence not optimized.

The last two rows in the table report results when we re-optimize the weight on the output gap (λ^a) given a weight of 0.077 for $(r_t^a - r^a)^2$ (next-to-last row) and 1 for $(\Delta r_t^a)^2$ (last row) in the loss function. As seen from the last column, these policies generate considerably lower interest volatility relative to the optimized loss function which excludes any interest rate terms, and the obtained std's are in line with even the three-std threshold applied by Adolfson et al. (2011). To compensate for the interest rate terms, the optimization generates a slightly higher λ^a compared to the simple loss function with the output gap only. Overall, the lower flexibility to adjust policy rates is associated with a lower welfare; the CEV roughly doubles in both cases.²⁵ But it is notable that the CEV does not increase to the same extent as $\text{std}(r_t^a)$ is reduced, reflecting that the central bank—which is assumed to operate under commitment—can still influence the long-term interest rate effectively by smaller but persistent movements of the short-term policy rate. Even so, we conclude that our benchmark result of a large weight on the real activity term holds up for a plausible degree of interest rate volatility.

5. Simple Interest Rate Rules

Up to this point, we have considered how simple mandates fare in terms of welfare and tried to find the best simple mandate among a certain class of such mandates. In this section, we turn our attention to simple interest rate rules. We do so for two reasons. First, we are interested in knowing to what extent simple interest rate rules can approximate the Ramsey policy compared with simple loss functions. Second, we are interested in knowing how a simple policy rule should be parameterized to *mimic* the Ramsey policy as closely as possible.

²⁵ It should be noted that the good performance of the nominal wage growth - labor gap simple mandate in Table 4 is also contingent on a relatively high interest rate volatility. However, when we augment the loss wage-labor loss function with an interest rate term, we find that the CEV is about twice as low as the inflation-output gap based objective which imposes the same interest rate volatility. Thus, the labor based mandate still outperforms the inflation-output gap mandate conditional on much less volatile policy rates.

To be concrete, the central bank is posited to implement monetary policy by following a certain simple interest rate rule. Once a rule is adopted the central bank is assumed to be able to choose the response coefficients in the simple rule to maximize household welfare. If we denote the solution as $X_t(R; X_{t-1})$, where R represent a specific policy rule, the optimized simple rule that maximizes household welfare is defined by

$$R^*(\Lambda) = \arg \min_{R \in \Lambda} E \left[(X_t(R; X_{t-1}))' W^{society} (X_t(R; X_{t-1})) \right], \quad (45)$$

where Λ is the set of possible parameterizations of the rule (45). The resulting loss for the society is

$$Loss^{rule}(\Lambda) = E \left[(X_t(R^*(\Lambda)))' W^{society} (X_t(R^*(\Lambda))) \right]. \quad (46)$$

Given our previous findings that an objective with inflation and the output gap provides a good approximation of household welfare, we consider variants of the following simple rule:

$$r_t^a - r^a = (1 - \rho_r) [\varrho_\pi (\pi_t^a - \pi^a) + \varrho_y (y_t^{gap}) + \varrho_{\Delta y} 4 \Delta y_t^{gap}] + \rho_r (r_{t-1}^a - r^a). \quad (47)$$

However, since the results in Table 4 showed that an objective with wage inflation and the hours gap provided an even better approximation of Ramsey policy, we also entertain variants of the following simple interest rate rule:

$$r_t^a - r^a = (1 - \rho_r) [\varrho_{\Delta w} (\Delta w_t^a - \Delta w^a) + \varrho_l (l_t^{gap}) + \varrho_{\Delta l} 4 \Delta l_t^{gap}] + \rho_r (r_{t-1}^a - r^a). \quad (48)$$

The results of this exercise are reported in Table 9. In the table, Panel A reports results when the objective is to minimize (46) and the rule is given by (47). Panel B, on the other hand, reports results when the rule is given by (48).

Turning to the results in the first panel in Table 9, we see that neither Taylor (1993) rule—which sets $\varrho_\pi = 1.5$, $\varrho_y = 0.5$ and $\varrho_{\Delta y} = \rho_r = 0$ in (47)—nor Taylor (1999) rule—which doubles ϱ_y to 1 instead—can approximate the Ramsey policy well using the 0.05 percent CEV cut-off value adopted by Schmitt-Grohe and Uribe (2007). Both policy rules increase CEV substantially relative to the simple mandate with inflation and output gap, which implied a loss of 0.044 percent relative to Ramsey. Perhaps counterintuitively to the simple mandate results that emphasized the importance of responding vigorously to economic activity, the Taylor (1999) rule is associated with higher loss than the Taylor (1993) rule. As can be seen from the third row in the table—which reports results for an optimized Taylor type rule—it seems as if the Taylor (1993) rule strikes a good compromise between responding to inflation and the output gap. Evidently, an optimized λ^a of unity in the

loss function 37 does not translate into equal coefficients for $\pi_t^a - \pi^a$ and y_t^{gap} in (47). When we re-optimize the coefficients while allowing for interest rate smoothing—the fourth row in the table—we see that welfare is improved somewhat, but not sufficiently to close the welfare gap to the optimized simple inflation-output gap mandate in Section 3.

The key to improve the welfare performance of the simple rule is to include the annualized growth rate of the output gap in the simple rule (fifth row). When doing so, we find that the $\varrho_{\Delta y}$ coefficient becomes extremely large (56.52) and that welfare is improved markedly. This finding is consistent with Orphanides and Williams (2008), who argued in favor of responding to the growth rate of the output gap in optimized simple rules within the context of learning and model uncertainty. However, we see from the last column that the standard deviation of the policy rate is substantially higher than the threshold value suggested by Adolfson et al. (2011) discussed earlier (see Section 4.3). And when we impose that the optimized rule should satisfy the constraint that $\text{std}(r_t^a)$ is lower or equal to 2.08 (i.e. the Adolfson et al. threshold which we used in Section 4.3), we find that the welfare gains are more modest (“Optimized, constr.”) relative to the unconstrained rule (“Optimized, uncon.”). Although this rule also features a very large long-term coefficient on the labor market gap (54.81), it should be noted that the short-term coefficient $((1 - \rho_r) \varrho_{\Delta y})$ is reduced sharply (from 29.4 to a meager 0.5).²⁶ Nevertheless, it is interesting to note that optimized simple rules perform about as well as their simple mandate peers when it comes to maximizing household welfare.

Table 9: Performance of Simple Rules (47).

Panel A: Inflation and Output Gap Rule (47)						
Parameterization	ϱ_π	ϱ_y	$\varrho_{\Delta y}$	ρ_r	CEV (%)	$\text{std}(r_t^a)$
Taylor (1993)	1.50	0.50	—	—	0.399	5.43
Taylor (1999)	1.50	1.00	—	—	0.768	7.53
Optimized, Taylor	2.23	0.49	—	—	0.254	4.30
Optimized, $\varrho_{\Delta y}=0$	11.78	5.76	—	0.99	0.216	2.08
Optimized, uncon.	20.20	0.40	56.52	0.48	0.033	7.81
Optimized, constr.	29.28	0.79	54.81	0.99	0.082	2.08

Panel B: Labor Market Rule (48)						
Parameterization	$\varrho_{\Delta w}$	ϱ_l	$\varrho_{\Delta l}$	ρ_r	CEV (%)	$\text{std}(r_t^a)$
Optimized, uncon.	49.18	1.74	204.59	0.71	0.014	7.83
Optimized, constr.	11.40	1.72	3.53	0.98	0.104	2.08

Note: The “Optimized” coefficients in the panels are found by maximizing household welfare, i.e. minimizing CEV. In the optimizations, we always constrain the smoothing coefficient ρ_r to be between 0 – 0.99. For the “Optimized,

²⁶ It is also important to point out that the size of $\varrho_{\Delta y}$ and the performance of the rule in terms of welfare are diminished if the policy maker responds to the actual growth rate instead of the change in the gap; according to the model it is crucial to take the growth rate in potential output into account.

constr.” optimizations, we have restricted the coefficients of the rule to imply a standard deviation for the policy rate less or equal to 2.0833.

Turning to Panel B in the table, we see that the performance of (48) is similar to the standard inflation-output gap based rule in Panel A. Unconstrained, the optimized rule calls for an extremely large response to the change in the labor gap. Interestingly, this unconstrained rule, which is associated with a CEV of a mere 0.0143 percent, performs better than any of the simple mandates or rules studied so far in the paper. However, a drawback with the optimized rule is the associated high interest rate volatility. And when imposing the restriction that $\text{std}(r_t^a)$ should be less than the Adolfson et al. threshold, the short- and long-term coefficients on the change in the labor gap are much smaller and the CEV of the rule deteriorates slightly below that found for the inflation-output gap based simple rule in Panel A. This finding demonstrates the importance of imposing reasonable constraints on the coefficients in the rule and suggests that some rules, which may perform very well in theory, may not be as desirable to implement in practice.

It is important to recognize that even if a certain set of variables perform well with simple objectives, the same set of variables may not perform well with simple interest rate rules. Our analysis shows that the mapping between interest rate rules and simple objectives is far from trivial. For instance, Table 2 reports that the optimized simple dual inflation-output gap mandate yields a loss of 0.0437. However, the third row in Table 9 shows that including the same variables results in an optimized simple interest rate rule for which the loss increases roughly five times to 0.2160, even when we allow for interest rate smoothing. Only when carefully designing the simple interest rate rule by including the change in the output gap (fourth row), does the optimized rule yield a welfare loss of 0.0331, which is lower than the loss of the optimized simple mandate.

These results demonstrate that inferring outcomes from simple mandates to simple interest rate rules can be difficult. We also show that both simple interest rate rules and simple mandates can perform very well; in particular, the optimal weight on economic activity is higher than conventionally thought in the previous literature. However, for each case, a careful examination of the relevant variables and the correct coefficients is always warranted.

6. Conclusions

- [Remains to be written.]

References

- Adjemian, Stéphane, Matthieu Darracq Pariès and Stéphane Moyen (2008), “Towards a Monetary Policy Evaluation Framework”, ECB Working Paper Series No. 942.
- Adolfson, Malin, Stefan Laséen, Jesper Lindé, and Lars E.O. Svensson (2011), “Monetary Policy Trade-Offs in an Estimated Open-Economy DSGE Model,” www.larseosvensson.net.
- Benigno, Pierpaolo and Michael Woodford (2006), “Linear-Quadratic Approximation of Optimal Policy Problems”, *Journal of Economic Theory* 147(1), 1–42.
- Bernanke, Ben S. (2013), “A Century of U.S. Central Banking: Goals, Frameworks, Accountability”, Remarks at “The First 100 Years of the Federal Reserve: The Policy Record, Lessons Learned, and Prospects for the Future” A conference sponsored by the National Bureau of Economic Research, Cambridge, Massachusetts.
- Blanchard, O., Galí, J. (2007), “Real Wage Rigidities and the New Keynesian Model,” *Journal of Money, Credit, and Banking* 39(1), 35–65.
- Bodenstein, Martin, James Hebden, and Ricardo Nunes (2012). “Imperfect Credibility and the Zero Lower Bound,” *Journal of Monetary Economics* 59(2), 135–149.
- Christiano, Lawrence, Martin Eichenbaum and Charles Evans (2005), “Nominal Rigidities and the Dynamic Effects of a Shock to Monetary Policy”, *Journal of Political Economy* 113(1), 1–45.
- Clarida, R., J. Galí, and M. Gertler (1999), “The Science of Monetary Policy: A New Keynesian Perspective,” *Journal of Economic Literature*, 37(4), 1661–1707.
- Debortoli, Davide, Junior Maih, and Ricardo Nunes (Forthcoming). "Loose Commitment in Medium-Scale Macroeconomic Models: Theory and Applications," *Macroeconomic Dynamics*.
- Dennis, Richard (2004), “Inferring Policy Objectives from Economic Outcomes”, *Oxford Bulletin of Economics and Statistics*, 66S, 735–764.
- Dotsey, Michael and Robert King (2005) “Implications of state dependent pricing for dynamic macroeconomic models”, *Journal of Monetary Economics* 52, 213–242.
- Erceg, Christopher J., Henderson, Dale W., Levin, Andrew T. (2000) “Optimal monetary policy with staggered wage and price contracts,” *Journal of Monetary Economics* 46, 281–313.
- English, William, Lopez-Salido, David, and Robert Tetlow (2013), “The Federal Reserve’s Framework for Monetary Policy – Recent Changes and New Questions”, manuscript, Federal Reserve Board.
- Galí, Jordi and Mark Gertler (1999), “Inflation Dynamics: A Structural Econometric Analysis”, *Journal of Monetary Economics*, 44, 195–220.
- Galí, Jordi, Mark Gertler, and David López-Salido (2001), “European Inflation Dynamics”, *European Economic Review*, 45, 1237–70.
- Galí, Jordi, Frank Smets, and Rafael Wouters (2011), “Unemployment in an Estimated New Keynesian Model”, *NBER Macroeconomics Annual*, 329–360.
- Galí, J. (2008) *Monetary Policy, Inflation and the Business Cycle: An Introduction to the New Keynesian Framework*, Princeton University Press, (Princeton, NJ).
- Galí, Jordi (2011) “Monetary Policy and Unemployment,” in B. Friedman and M. Woodford (eds.) *Handbook of Monetary Economics*, vol. 3A, Elsevier B.V., 487–546.
- Ilbas, Pelin (2008), “Estimation of Monetary Policy Preferences in a Forward-Looking Model: A Bayesian Approach”, National Bank of Belgium Working Paper Series No. 129.

- Ilbas, Pelin (2012), “Revealing the preferences of the U.S. Federal Reserve,” *Journal of Applied Econometrics* 27(3), 440-473.
- Jensen, Christian and Bennett T. McCallum (2010), “Optimal Continuation versus the Timeless Perspective in Monetary Policy”, *Journal of Money, Credit and Banking* 42(6), 1093–1107.
- Jensen, Henrik (2002), “Targeting Nominal Income Growth or Inflation?”, *American Economic Review* 92(4), 928–956.
- Jung, Yong-Gook and Muenchika Katayama (2012), “Uncovering the Fed’s Preferences”, Working Paper.
- Justiniano, Alejandro, Giorgio E. Primiceri, and Andrea Tambalotti (2013), “Is There A Trade-Off Between Inflation and Output Stabilization”, *American Economic Journal: Macroeconomics* 5(2), 1-31.
- Leeper, Eric and Tao Zha (2003), “Modest Policy Interventions”, *Journal of Monetary Economics* 50(8), 1673–1700.
- Levin, Andrew, López-Salido, J David and Tack Yun (2007), “Strategic Complementarities and Optimal Monetary Policy”, CEPR Discussion Papers No. 6423.
- Levine, Paul, Peter McAdam, and Joseph Pearlman (2008), “Quantifying and Sustaining Welfare Gains from Monetary Commitment”, *Journal of Monetary Economics* 55, 1253–1276.
- Lucas, Robert E., Jr., (1987), *Models of Business Cycles*, Basil Blackwell, New York.
- Marcet, Albert and Ramon Marimon (2012), "Recursive Contracts" Working Paper, European University Institute.
- Orphanides, Athanasios and John C. Williams (2008) “Learning, Expectations Formation, and the Pitfalls of Optimal Control Monetary Policy”, *Journal of Monetary Economics* 55, S80-S96.
- Otrok, Christopher, (2001) “On measuring the welfare cost of business cycles,” *Journal of Monetary Economics* 47(1), 61-92.
- Persson, Torsten, and Guido Tabellini (1993). “Designing Institutions for Monetary Stability,” *Carnegie-Rochester Conference Series on Public Policy* 39(1), 53-84.
- Plosser, Charles I. (2014), “Shocks, Gaps, and Monetary Policy”, Remarks at the KAEA-Maekyung Forum, Philadelphia.
- Reifschneider, David, William L. Wascher, and David W. Wilcox (2013), “Aggregate Supply in the United States: Recent Developments and Implications for the Conduct of Monetary Policy”, manuscript, Federal Reserve Board.
- Rogoff, Kenneth (1985). “The Optimal Degree of Commitment to an Intermediate Monetary Target,” *Quarterly Journal of Economics* 100(4), 1169-89.
- Rotemberg, Julio J. and Michael Woodford (1998), “An Optimization-Based Econometric Framework for the Evaluation of Monetary Policy: Expanded Version”, NBER Technical Working Paper 0233.
- Rudebusch, Glenn and Lars E.O. Svensson (1999), “Policy Rules for Inflation Targeting” in John B. Taylor, ed., *Monetary Policy Rules*, University of Chicago Press.
- Schmitt-Grohe, Stephanie, and Martin Uribe (2007), “Optimal, Simple, and Implementable Monetary and Fiscal Rules”, *Journal of Monetary Economics* 54, 1702-1725.
- Smets, Frank and Raf Wouters (2003), “An Estimated Stochastic Dynamic General Equilibrium Model of the Euro Area”, *Journal of the European Economic Association* 1(5), 1123–1175.

- Smets, Frank and Raf Wouters (2007), “Shocks and Frictions in U.S. Business Cycles: A Bayesian DSGE Approach”, *American Economic Review* 97(3), 586–606.
- Svensson, Lars E.O. (1997), “Inflation Forecast Targeting: Implementing and Monitoring Inflation Targets,” *European Economic Review* 41, 1111–1146.
- Svensson, Lars E.O. (2010), “Inflation Targeting,” in Friedman, Benjamin M., and Michael Woodford, eds., *Handbook of Monetary Economics*, Volume 3B, chapter 22, Elsevier.
- Svensson, Lars E.O. (2011), “Practical Monetary Policy: Examples from Sweden and the United States,” *Brookings Papers on Economic Activity*, 289–332.
- Taylor, John B. (1993). “Discretion versus Policy Rules in Practice”. *Carnegie-Rochester Conference Series on Public Policy* 39: 195–214.
- Taylor, John B., 1999. “The robustness and efficiency of monetary policy rules as guidelines for interest rate setting by the European central bank,” *Journal of Monetary Economics* 43(3), 655–679.
- Taylor, John and John Williams (2011), “Simple and Robust Rules for Monetary Policy”, in B. M. Friedman and M. Woodford (eds.) *Handbook of Monetary Economics*.
- Vestin, David (2006) “Price-level versus inflation targeting”, *Journal of Monetary Economics* 53, 1361–1376.
- Walsh, Carl E. (2003), “Speed Limit Policies: The Output Gap and Optimal Monetary Policy”, *American Economic Review* 93(1), 265–278.
- Walsh, Carl E. (2005), “Endogenous Objectives and the Evaluation of Targeting Rules for Monetary Policy”, *Journal of Monetary Economics* 52, 889–911.
- Woodford, Michael, 2003, *Interest and Prices*, Princeton: Princeton University Press.
- Yellen, Janet L. (2012), “The Economic Outlook and Monetary Policy”, Remarks at the Money Marketmakers of New York University, New York.
- Yun, Tack (1996), “Nominal Price Rigidity, Money Supply Endogeneity, and Business Cycles”, *Journal of Monetary Economics* 37, 345–370.